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Influence of Fiber Properties on Shear Failure of Steel Fiber Reinforced Beams Without Web Reinforcement: ANN Modeling

Abstract

In this paper, an artificial neural network (ANN-10) model was developed to predict the ultimate shear strength of steel fiber reinforced concrete (SFRC) beams without web reinforcement. ANN-10 is a four-layered feed forward network with a back propagation training algorithm. The experimental data of 70 SFRC beams reported in the technical literature were utilized to train and test the validity of ANN-10. The input layer receives 10 input signals for the fiber properties (type, aspect ratio, length and volume content), section properties (width, overall depth and effective depth) and beam properties (longitudinal reinforcement ratio, compressive strength of concrete and shear span to effective depth ratio). ANN-10 has exhibited excellent predictive performance for both training and testing data sets, with an average of 1.002 for the average of predicted to experimental values. This performance of ANN-10 established the promising potential of Artificial Neural Networks (ANNs) to simulate the complex shear behavior of SFRC beams. ANN-10 was applied to investigate the influence of the fiber volume content, type, aspect ratio and length on the ultimate shear strength of SFRC.

Keywords

Beams, Fiber reinforced concrete, Shear failure, Steel fiber reinforced concrete (SFRC), Numerical modeling.

Yassir M. Abbas [a, 1]
M. Iqbal Khan [a, 2 *]

[a] Department of Civil Engineering, King Saud University, Riyadh, P. O. Box 800, Riyadh 11421, Saudi Arabia

[1] Email: yabbas@ksu.edu.sa
[2] Email: miqbal@ksu.edu.sa
* Corresponding author

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1 INTRODUCTION

Reinforced concrete beams with or without web reinforcement, which are subjected to combined flexural and shear stress, can be prone to instantaneous failure in shear (Roberts and Ho 1982; Dinh 2009). Traditionally, reinforced concrete beams are reinforced with web reinforcement to avoid failure due to tensile-shear stresses. The inclusion of short and discrete steel fibers with an aspect ratio

(fiber length to diameter) ranging between 20 to 100 in concrete, has been proven to enhance the shear strength by resisting the formation and growth of cracks (Al-Ta'an and Al-Feel 1990). The use of fibers in thin sections and congested reinforcing steel sections is highly beneficial, as it may be difficult to provide conventional web reinforcement. For deep beams and due to the high inclined tensile stresses arising from the shear stresses on vertical planes, shear cracks may propagate rapidly in the web causing a catastrophic failure. However, the understanding of the shear behavior of beams, particularly for deep beams, constitutes a challenging engineering problems, since various modes of failures have been observed for such beams (Roberts and Ho 1982). This problem is complicated by the nonlinear interactions arising from the inclusion of steel fiber in concrete. At present, numerous predictive models for the evaluation of the ultimate shear strength of SFRC beams have been developed based on the regression analysis (Mansour et al. 1986; Sharma 1986; Al-Ta'an and Al-Feel 1990; Khuntia et al. 1999). In such complex problems, which are difficult to be modeled using conventional modeling techniques, the application of ANNs may have a good application potential. ANNs have been introduced to the field of civil engineering as a powerful modeling technique, which has achieved acceptable success in many applications (Hegazy et al. 1998; Perera et al. 2010; Bashir and Ashour 2012; Mashrei et al. 2013; Lee and Lee 2014). ANNs are numerical architectures composed of huge elements of strongly interlocking manufactured elements known as neurons, which simulate the human brain mechanism of learning and solving problems. The construction of the ANN models mainly depends on the actual, adequate and reliable experimental data. ANNs can solve highly non-linear and sophisticated problems, including problems having inaccurate and scattered data (Jha 2007).

In the present literature, the information concerning the use of ANN for the prediction of the ultimate shear strength of SFRC beams is scarce. Naik and Kute (2014) developed an ANN model based on seven and eight input nodes for the prediction of high performance deep SFRC beams. These researchers have used the developed ANN to investigate the influence of the shear span to effective depth ratio of high performance deep SFRC beams. They reported that ANNs are a promising technique to predict the complex shear behavior of SFRC beams in terms of various parameters, which can reduce the cost of the experimental investigations. Using four and five input node ANNs, Adhikari and Mutsuyoshi (2006) predicted the ultimate shear strength of SFRC beams based on the experimental results of the literature. It was reported that the predictive efficiency of the network enhances as the number of input nodes increases. In addition, it was observed that ANNs have better predictive performance compared to regression methods. It is worth noting that considerable research effort has been undertaken to investigate the effects of incorporating steel fibers on the ultimate shear strength of SFRC beams based on the fiber factor, which combines the fiber properties (type, length and aspect ratio). Few reported experimental investigations are available concerning the effect of the fiber volume content on the ultimate shear strength of SFRC with or without web reinforcement (Lim and Oh 1999; Kwak et al. 2002; Cucchiara et al. 2004). In addition, very few researchers have investigated the influence of the individual fiber properties on the ultimate shear strength of SFRC beams without web reinforcement (Dinh 2009). The objectives of this study are: 1) to investigate the potential of using ANNs for the prediction of the ultimate shear strength of SFRC beams, and 2) to investigate the influence of the fiber properties on the ultimate strength of SFRC beams without web reinforcement.

2 SIGNIFICANCE OF RESEARCH

Concrete as a brittle material responds by cracking when subjected to low tensile stresses arising from the shear stresses at the inclined sections of a beam. The failure of beams usually causes catastrophic loss, both human and material, because of its sudden occurrence without a warning. The incorporation of steel fibers in concrete enhances its tensile stress resistance at the post cracking stage of concrete, which increases the ultimate shear strength of SFRC beams. However, the only accurate method for the evaluation of this strength is through the costly experimental testing of full-scale beams. The development of rational numerical methods for the prediction of the fracture behavior of SFRC reduces the cost of experimentation and provides the appropriate tool for the optimal design of SFRC. In addition, investigating the role of the individual fiber properties assists in providing an understanding of the behavior of SFRC beams in shear.

3 PARAMETERS INFLUENCING THE ULTIMATE SHEAR STRENGTH OF SFRC

As a conventional reinforced concrete, the ultimate shear strength of SFRC beams without web reinforcement is primarily influenced by: 1) the compressive strength of concrete, 2) the ratio of the longitudinal reinforcement, 3) the shear span to effective depth ratio, and 4) the section dimensions (particularly the effective depth). In addition, the ultimate shear strength of SFRC beams are affected by the properties of the fiber, namely: 1) type, 2) length, 3) aspect ratio, and 4) volume content. Various researchers assumed that the shear resistance of SFRC beams without web reinforcement is based on: 1) the shear force in the untracked compression zone, 2) the aggregate interlock force in the cracked tensile concrete, 3) the dowel force in the main steel, and 4) the contribution of steel fibers in the diagonal crack zone (Al-Ta'an and Al-Feel 1990; Lim and Oh 1999; Dinh 2009). Figure 1 shows the shear resistance forces at the inclined tensile crack of SFRC beam without web reinforcement.

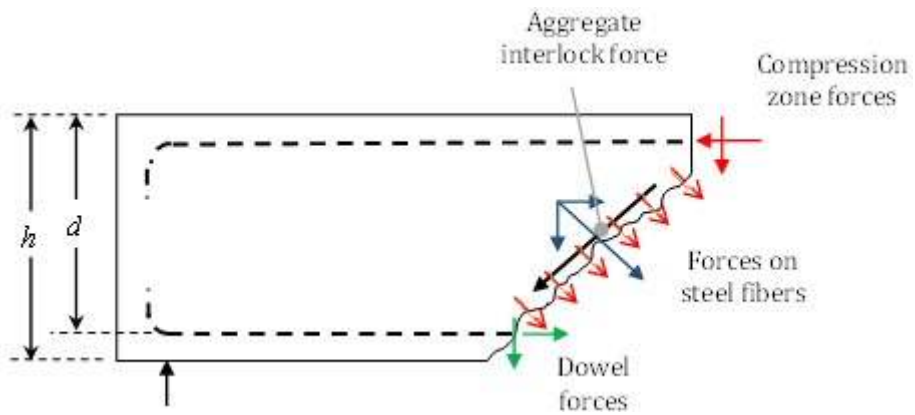

Figure 1: Shear resistance forces at inclined tensile crack of SFRC beam without web

Based on experimental investigations, Khuntia et al. (1999) reported that increasing the compressive strength of concrete drastically enhances the ultimate shear strength of SFRC beams. This was attributed to the enhancement occurring in the fiber-matrix interfacial bond. In contrast, in-

creasing the shear span to an effective depth ratio drastically reduces the ultimate shear strength of SFRC beams due to the arching behavior. Swamy and Bahia (1985) observed that, the ultimate shear strength of SFRC beams increases as the longitudinal reinforcement increases to a particular value beyond which it decreases. This was attributed to the increase in the longitudinal reinforcement-concrete dowel interactions. The fiber aspect ratio was not reported to affect the ultimate shear strength of SFRC beams. However, various researchers investigated the effect of fiber using the fiber factor suggested by Narayanan and Darwish (1987), which combines the fiber type, aspect ratio and volume content. As reported by these researches, the most significant factor is the fiber volume content.

4 ARTIFICIAL NEURAL NETWORKS

In the field of civil engineering, ANNs have achieved a high degree of applicability. Sanand and Saka (2001) developed an ANN to predict the ultimate shear strength of conventional reinforced concrete deep beams. These researchers have shown that the developed ANN has better predictive capability than the equations suggested by the ACI 318 committee. Hegazy et al. (1998) investigated the potential of using ANNs to develop efficient predictive models for the structural behavior of concrete slabs. They reported that ANNs are a useful technique for the reasonable prediction of the behavior of concrete slabs without additional experimental testing.

Due to its simplicity, the multi-layer perceptron ANNs with feed forward and back propagation are mostly utilized in engineering. The input layer receives signals, which treated through the hidden layer, and finally produced in the output layer. The learning process requires the evaluation of the weight of the processing connections and their modality. Mostly, only one hidden layer is enough to correlate highly nonlinear parameters, however, in some cases two or more hidden layers are more efficient (Adhikary and Mutsuyoshi 2006). The major concerns of structural analysis problems, such as predicting different properties of concrete and load carrying capacity, have been solved mostly by using back propagation (Naik and Kute 2014).

5 DEVELOPMENT OF THE NEURAL NETWORK MODEL

In this paper, a multilayer feed forward neural network with a back propagation training algorithm was used to develop ANN-10. Figure 2 shows the topology of ANN-10, which has 10 input nodes, two hidden layers with 14 neurons and one output layer. In this figure, the network is represented in the form of a directed graph, in which the nodes represent the processing unit, the straight lines represent the connections, and the arrowhead lines indicate the normal direction of signal flow. In addition, $w_{x,n}$ and $v_{n,y}$ are the weight matrices and b_1 to b_{10} are the bias vector elements.

In order to achieve the desired outputs, weights (represent connection strength between neurons) and biases were corrected at a constant learning rate using the perceptron learning rule as given by Eqs. (1)-(2). Then, the network error (the difference between calculated and expected target patterns) was back propagated from the output layer to the input layer. The process of correcting the neuron weights and biases was undertaken until the network output arrives at a specific level of accuracy. Once the activities of all the output units were determined, the network computed the errors E, which is defined by Eq. (3).

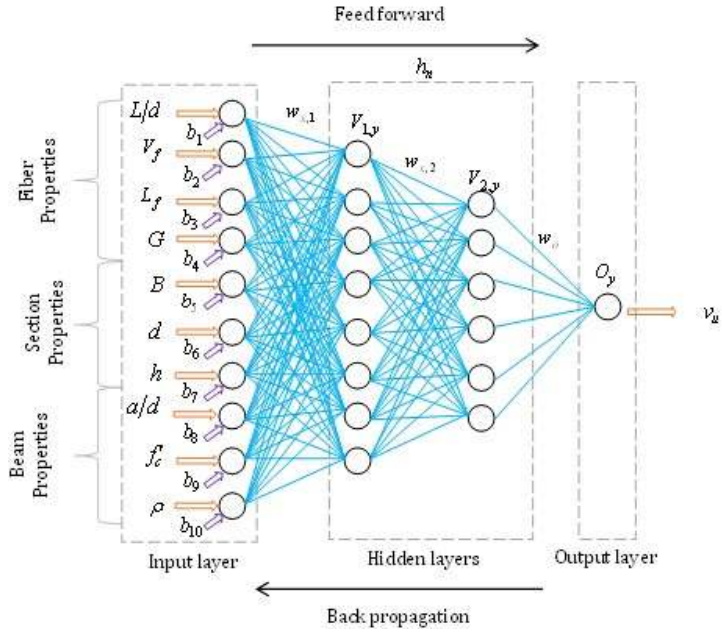

Figure 2: The topology of ANN-10

To accelerate the convergence of the predicted output with the desired output, a sigmoid activation function, $\phi(V)$ as given by Eq. (4), was used to evaluate the values of the hidden and output neurons. Before applying the sigmoid activation function, a linear normalization function, as given by Eq. (5), was applied to scale the input values between zero and one. Eqs. (6)-(7) describes the mode of mathematical operations in the hidden and output layers of ANN-10. It is worth noting that MS Excel was utilized to develop the ANN-10 based on the flow chart given in Figure 3. Moreover, the Optimization Modeling System "Solver" in the MS Excel was used to optimize the developed ANN model. The parameters of the Solver tool were adjusted arbitrary and those result in the minimum mean square error (E in Eq. 3) were adopted.

$$w_i(t+\Delta t) = w_i(t) + \Delta w_i(t) \tag{1}$$

$$\Delta w_i(t) = \gamma(D-Y)I_i \tag{2}$$

$$E = \sum_i (D_i - Y_i)^2 \tag{3}$$

$$\phi(V) = \frac{1}{1+e^{-\lambda V}} \tag{4}$$

$$S = \frac{I - I_{\min}}{I_{\max} - I_{\min}} \tag{5}$$

$$h_n = \phi(V_n) = \phi\left(\sum_{x=0}^{M} w_{n,x} i_x\right) = \phi\left(\sum_{x=1}^{M} w_{n,x} i_x + b_n\right) \tag{6}$$

$$O_n = \phi(V_y) = \phi\left(\sum_{x=0}^{N} v_{y,n} h_n\right) = \phi\left(\sum_{x=0}^{N} v_{y,n} h_n + b_y\right) \tag{7}$$

In Eqs. (1)-(7), t stands for time, D is the desired output, Y is the actual output, I_i is the ith input signal, γ is the learning rate, V is the value of the normalized input or output, i_x is the transmitted value from x^{th} input neuron, i^{th}, h_n is the activity level generated at the nth hidden neuron, O_n is the activity level generated at the yth output neuron, $w_{n,x}$ and $v_{y,n}$ are weights on the connections to the hidden and output layers of neurons, respectively. Finally, b_n, b_y and $\phi(V)$ are weighted biases and activation function.

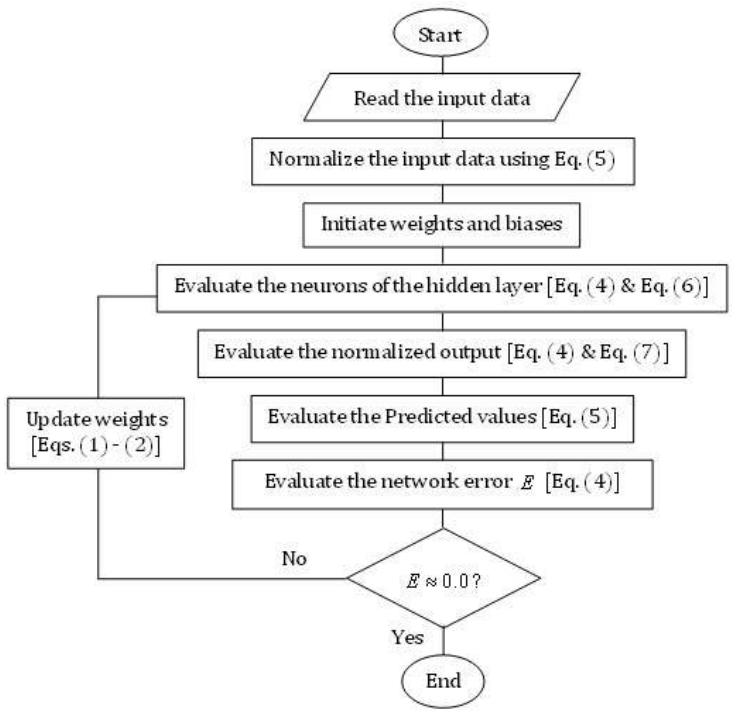

Figure 3: Flow chart for development of ANN-10

6 EXPERIMENTAL DATA

In this study, the experimental data utilized to train and test the performance of ANN-10 were the experimental test results of 70 SFRC beams collected from 11 published reports (Roberts and Ho 1982; Swamy and Bahia 1985; Lim et al. 1987; Swamy et al. 1993; Tan et al. 1993; Adebar et al. 1997; Lim and Oh 1999; Kwak et al. 2002; Cucchiara et al. 2004; Parra-Montesinos 2006; Dinh 2009) as given in Table 1. The collected data included: 1) G (the fiber geometry code, which is 1 for straight, 2 for crimped, 3 for hooked fibers), 2) V_f (the fiber volume content), 3) L_f / d_f (the fiber aspect ratio), 4) L_f (the fiber length), 5) h (the beam section overall depth), 6) b (the beam

section width), 7) d (the beam section effective depth), 8) a/d (the shear span to effective depth ratio), 9) ρ (the ration of the longitudinal reinforcement, 10) f_c' (the concrete compressive strength) and 11) $v_u = V_u/bh$ (the ultimate shear strength of the beam).

It should be noted that the cylindrical compressive strength of concrete was evaluated as 80% of the cubic compressive strength. Data pre-processing was carried out on the collected results of the experimental data to exclude the inconsistent data points. As the objective of this paper is to predict the ultimate shear strength of FRC beams without web reinforcement, beams that failed in the flexure mode were excluded. In addition, high strength and ultra-high beams having high strength and ultra-high compressive strength concrete $\left(f_c' > 60\,\text{MPa}\right)$ were also excluded. Then, the collected data were subdivided into two sets, 70% for the training data set (49 data points), and 30% for the testing data set (21 data points).

No	L_f/d_f	ρ_f (%)	L_f (mm)	G	h (mm)	b (mm)	d (mm)	$f_{c'}$ (MPa)	a/d	ρ (%)	v_u	Ref.
1	60	1.00	42	1	180	100	140	38.69	0.31	2.23	4.490	Lim and Oh 1999
2	100	0.00	38	1	200	50	170	31.36	2.41	2.10	2.760	Roberts and Ho 1982
3	100	0.85	38	1	200	50	170	31.28	2.41	2.10	3.860	
4	100	1.30	38	1	200	50	170	59.88	2.41	2.10	4.260	
5	100	0.00	38	1	200	50	170	31.36	1.62	2.10	5.330	
6	100	0.85	38	1	200	50	170	31.28	1.62	2.10	5.990	
7	60	1.00	30	3	250	150	219	40.85	2.80	6.59	2.934	Cucchiara et al. 2004
8	60	2.00	30	3	250	150	219	43.23	2.80	6.59	3.145	
9	60	1.00	30	3	250	150	219	40.85	2.00	6.59	3.503	
10	60	2.00	30	3	250	150	219	43.23	2.00	6.59	3.516	
11	60	1.00	30	3	457	152	381	38.10	3.50	1.96	3.030	Parra-Montesinos 2006
12	60	1.00	30	3	457	152	381	38.10	3.50	1.96	3.090	
13	60	1.00	30	3	457	152	381	38.10	3.50	2.67	3.460	
14	60	1.00	30	3	457	152	381	38.10	3.50	2.67	2.530	
15	60	1.50	30	3	457	152	381	31.00	3.40	2.67	2.560	
16	60	1.50	30	3	457	152	381	31.00	3.40	2.67	3.370	
17	60	1.50	30	3	457	152	381	49.90	3.40	2.67	3.280	Parra-Montesinos 2006
18	60	1.50	30	3	457	152	381	49.90	3.40	2.67	3.260	
19	60	1.00	30	3	457	152	381	49.20	3.40	2.67	2.970	
20	60	1.00	30	3	457	152	381	49.20	3.40	2.67	3.770	
21	60	0.75	30	3	610	152	558	54.10	1.60	2.12	3.240	Adebar et al. 1997
22	60	1.50	30	3	610	152	558	49.90	1.60	2.12	3.810	
23	60	0.40	30	3	610	152	558	54.80	1.60	2.12	2.400	
24	60	0.60	30	3	610	152	558	56.50	1.60	2.12	2.730	
25	100	0.40	50	3	610	152	558	46.90	1.60	2.12	2.900	
26	100	0.60	50	3	610	152	558	40.80	1.60	2.12	2.790	
27	63	0.50	50	3	250	125	212	63.80	2.00	1.46	5.090	Kwak et al. 2002
27	63	0.50	50	3	250	125	212	63.80	2.00	1.46	5.090	

Table 1: Experimental data.

No	L_f/d_f	ρ_f (%)	L_f (mm)	G	h (mm)	b (mm)	d (mm)	$f_{c'}$ (MPa)	a/d	ρ (%)	v_u	Ref.
28	63	0.75	50	3	250	125	212	68.60	2.00	1.46	5.440	Kwak et al. 2002
29	63	0.50	50	3	250	125	212	63.80	3.00	1.46	3.090	
30	63	0.75	50	3	250	125	212	68.60	3.00	1.46	3.400	
31	63	0.50	50	3	250	125	212	63.80	4.00	1.46	2.410	
32	63	0.75	50	3	250	125	212	68.60	4.00	1.46	2.740	
33	63	0.50	50	3	250	125	212	30.80	4.00	1.46	4.040	
34	63	0.50	50	3	250	125	212	30.80	2.00	1.46	2.550	
35	63	0.50	50	3	250	125	212	30.80	3.00	1.46	2.000	
36	60	0.50	30	3	375	60	340	35.0	2.00	3.44	5.340	
37	60	0.75	30	3	375	60	340	33.0	2.00	3.44	4.430	Tan et al. 1993
38	60	1.00	30	3	375	60	340	36.0	2.00	3.44	5.150	
39	60	1.00	30	3	375	60	340	36.0	2.50	3.44	3.780	
40	60	0.50	30	3	152	254	221	34.0	1.50	2.39	4.000	Lim et al. 1987
41	60	1.00	30	3	152	254	221	34.0	1.50	2.39	4.380	
42	60	1.00	30	3	152	254	221	34.0	2.50	2.39	2.450	
43	60	1.00	30	3	152	254	221	34.0	3.50	2.39	2.000	
44	80	1.50	76	2	610	305	546	32.8	2.80	1.84	2.030	Parra-Montesinos 2006
45	100	0.40	50	2	250	175	210	35.5	4.50	4.00	2.160	Swamy and Bahia 1985
46	100	0.80	50	2	250	175	210	37.4	4.50	4.00	3.100	
47	100	1.20	50	2	250	175	210	39.8	4.50	4.00	3.130	
48	100	1.00	50	2	300	55	265	40.9	3.40	4.31	4.030	Swamy et al. 1993
49	100	1.00	50	2	300	55	265	36.0	4.90	4.31	2.900	
50	100	1.00	50	2	300	55	265	37.8	2.00	2.76	4.910	
51	100	1.00	50	2	300	55	265	35.7	2.00	1.55	4.630	
52	55	0.75	30	3	457	152	381	44.8	3.43	1.96	2.940	Dinh 2009
53	55	0.75	30	3	457	152	381	44.8	3.43	1.96	2.750	
54	55	1.00	30	3	457	152	381	38.1	3.50	1.96	3.030	
55	55	1.00	30	3	457	152	381	38.1	3.50	1.96	3.100	
56	55	1.50	30	3	457	152	381	38.1	3.43	2.67	3.380	
57	55	1.50	30	3	457	152	381	45.0	3.43	2.67	3.280	
58	55	1.50	30	3	457	152	381	45.0	3.43	2.67	3.260	
59	80	1.00	60	3	457	152	381	49.2	3.43	2.67	3.770	
60	80	0.75	30	3	457	152	381	43.4	3.43	1.96	3.310	
61	55	0.75	30	3	689	203	457	50.8	3.50	2.06	2.930	
62	80	0.75	60	3	689	203	457	28.8	3.50	2.06	2.810	
63	55	0.75	30	3	689	203	457	42.3	3.50	1.56	2.780	
64	80	0.75	60	3	689	203	457	29.6	3.50	1.56	2.140	
66	80	0.75	60	3	689	203	457	29.6	3.50	1.56	1.790	
66	55	1.5	30	3	689	203	457	44.5	3.50	2.06	3.50	
67	55	1.50	30	3	457	152	381	38.1	3.43	2.67	2.560	
68	100	0.80	50	2	250	175	210	38.2	4.50	3.05	3.210	
66	100	1.00	50	2	300	55	265	35.6	2.00	4.31	5.480	
70	100	1.00	50	2	300	55	265	33.1	3.40	2.76	3.110	
71	100	1.00	50	2	300	55	265	35.9	4.90	2.76	2.920	

Table 1: Experimental data (contd.).

Table 2 presents the range, arithmetic mean (μ), standard deviation (σ) and the coefficient of variance (COV) of the collected data.

	L_f/d_f	ρ_f (%)	L_f (mm)	G	h (mm)	b (mm)	d (mm)	$f_{c'}$ (MPa)	a/d	ρ (%)	v_u (MPa)
Training data											
No.	49	49	49	49	49	49	49	49	49	49	49
Min.	55	0.00	30	1	152	50	140	30.80	0.31	1.46	2.000
Max.	100	2.00	60	3	610	254	558	68.60	4.00	6.59	5.990
range	45	2.00	30	2	458	204	418	37.80	3.69	5.13	3.990
μ	66	0.94	36	3	364	144	319	44.04	2.75	2.51	3.346
σ	14.69	0.44	9	0.66	148	46	124.5	11.23	0.89	1.30	0.850
COV	0.22	0.47	0.25	0.24	0.41	0.32	0.39	0.26	0.32	0.52	0.260
Testing data											
No.	21	21	21	21	21	21	21	21	21	21	21
Min.	55	0.40	30	2	250	55	210	28.80	2.00	1.55	2.030
Max.	100	1.50	76	3	689	305	546	50.80	4.90	4.31	5.480
range	45	1.10	46	1	439	250	336	22.00	2.90	2.76	3.450
μ	83	0.93	46	2	412	126	328	36.89	3.30	2.99	3.546
σ	19.59	0.27	12.76	0.51	176	79	104	4.92	1.05	0.98	1.07
COV	0.24	0.29	0.28	0.21	0.43	0.63	0.32	0.13	0.32	0.33	0.30

Table 2: Statistics of experimental data

7 RESULTS AND DISCUSSION

7.1 Analysis and Validity of the Model

The performance of ANN-10 was evaluated by conducting error analysis. Table 3 shows the summary of the error analysis of ANN-10 for the training and testing data sets. In this table, the minimum, maximum, μ , σ and COV are given for: 1) the square error, 2) the absolute error and 3) the predicted to experimental values. For the training data set, the average of square error, absolute error and predicted to experimental values ratio were 0.032, 0.106, and 1.002, respectively. However, they were 0.029, 0.112 and 1.002, respectively, for the testing data set. Figure 4~5 show the performance of ANN-10 in predicting the ultimate shear strength of SFRC beams for the training and testing data sets, respectively. From Figure 4 and Figure 5, it can be seen that ANN-10 has excellent predictive performance for the prediction of the training and testing data sets with more than 95% correlation coefficient. These strong correlations establish the validity of ANN-10 for the prediction of the ultimate shear strength of SFRC without web reinforcement.

		Training data set	Testing data set
Square error	Min.	15.1451×10^{-6}	0.251×10^{-6}
	Max.	0.248	0.179
	μ	0.032	0.029
	σ	0.067	0.048
	COV.	2.088	1.676
Absolute error	Min.	38.913×10^{-3}	5.006×10^{-3}
	Max.	0.498	0.424
	μ	0.106	0.112
	σ	0.144	0.127
	COV.	1.366	1.138
Predicted/Experimental	Min.	0.856	0.918
	Max.	1.181	1.076
	μ	1.002	1.002
	σ	0.060	0.037
	COV.	0.059	0.037

Table 3: Summary of error analysis.

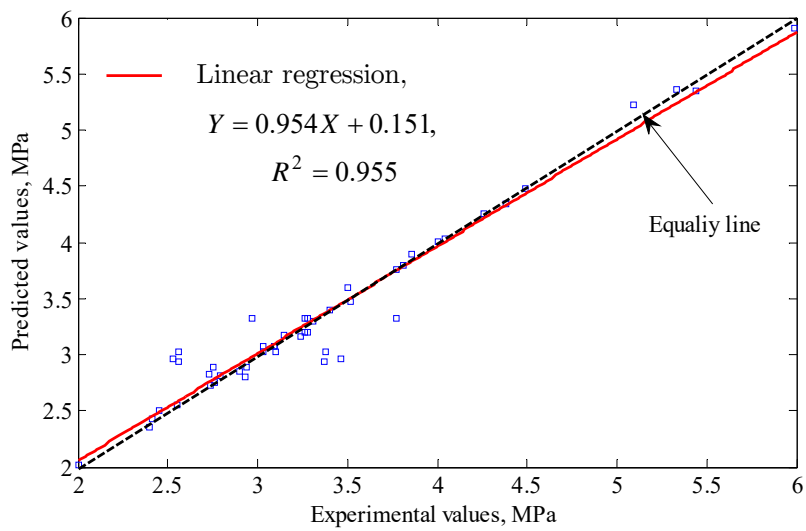

Figure 4: Experimental values vs. predicted values of ultimate shearing strength for the training data set

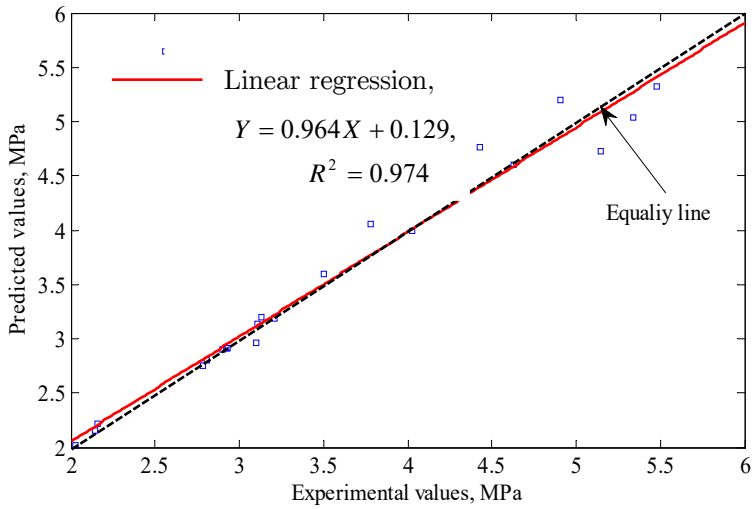

Figure 5: Experimental values vs. predicted values of ultimate shearing strength for the testing data set

7.2 Parametric Study

The network ANN-10 was utilized to study the influence of the individual properties of the fiber on the ultimate shear strength of SFRC beams without web reinforcement. At different shear span to effective depth ratios a/d, the effect of fiber volume content, aspect ratio and length were studied by varying their values. To investigate the influence of the type of fiber, the fiber geometry code was kept constant for different shear spans to effective depth ratios.

7.2.1 Influence of Volume Content of Fibers

Figure 6 shows the influence of V_f on v_u for SFRC beams without web reinforcement for different a/d values. The kept-constant properties of the investigated beams are shown in this figure. For deep beams ($a/d \le 2$), it can be seen from this figure that v_u drastically increases as V_f increases to a certain value (about 1%), after which v_u increases marginally. However, for shallow beams ($a/d > 2$), little improvement of v_u with increasing V_f was observed. It is worth noting that a similar behavior for SFRC beams was reported by Lim and Oh (1999), and Cucchiara et al. (2004). They showed that the inclusion of an appropriate volume content of steel fiber could increase the ultimate shear strength more than the flexural strength of longitudinally reinforced SFRC beams, which alters the ductile shear failure mode into the flexure model of failure.

In addition from Figure 6, it can be seen that for $V_f < 0.5\%$, v_u increases as a/d increases, however, this behavior is changed for $V_f > 0.5\%$. In other words, for $V_f < 0.5\%$ the shallower beam (has the largest a/d) has the highest v_u compared to other beams. However, for $V_f > 0.5\%$ the deeper beam (has the smallest a/d) has the highest v_u. This finding demonstrates that the addition of about 0.5% or more steel fibers in reinforced concrete beams alters the brittle shear behavior and

sudden failure of beams, especially for deep beams ($a/d \leq 2.0$). In addition, this result confirms the capability of steel fibers to increase the ultimate shear strength of beams, in a way that they can replace the nominal web reinforcement as reported by various researchers (Furlan and de Hanai 1997; Imam et al. 1997; Lim and Oh 1999; Dinh 2009). The improvement in v_u due to the increase V_f is attributed to the increase in the crack bridging capacity at the post-cracking stage, which enhances the overall mechanical performance of the concrete.

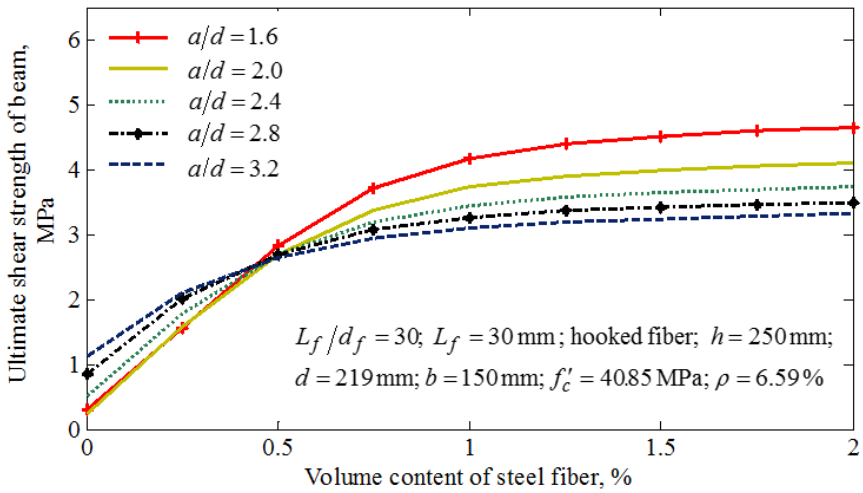

Figure 6: Influence of volume content of fiber on the ultimate shear strength of SFRC beams without web reinforcement

7.2.2 Influence of Aspect Ratio of Fibers

Figure 7 shows the influence of L_f/d_f on v_u of SFRC beams without web reinforcement for different a/d values. The constant properties of the studied SFRC beams are given in this figure. As can be seen from this figure, increasing L_f/d_f from 60 to 100 causes a 24~32% increase for v_u of shallow and deep beams. In addition, the improvement of v_u due to increasing L_f/d_f in deep beams are more than the same for shallow beams. The improvement in v_u due to an increase in L_f/d_f is attributed to the increase in the fiber-concrete matrix interface.

7.2.3 Influence of Length of Fibers

Figure 8 shows the influence of L_f on v_u of SFRC beams without web reinforcement for different a/d values. The properties of the studied SFRC beams are given in this figure. As can be seen from this figure, increasing L_f from 30 to 60 causes a 5~20% increase in v_u for deep and shallow beams. Unlike the change in v_u due to L_f/d_f, the percentage increase in v_u for shallow beams is more than that for deep beams. This demonstrates that the influence of L_f is more pronounced for shallow

beams compared to deep beams. For these particular SFRC beams, it seems that the optimum fiber length for the investigated beam is 45mm.

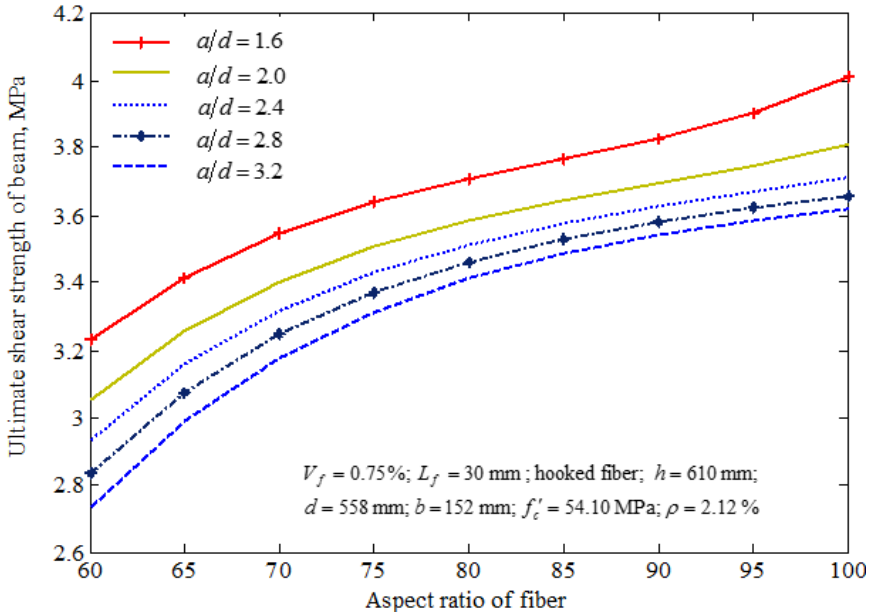

Figure 7: Influence of aspect ratio of fiber on the ultimate shear strength of SFRC beams without web reinforcement

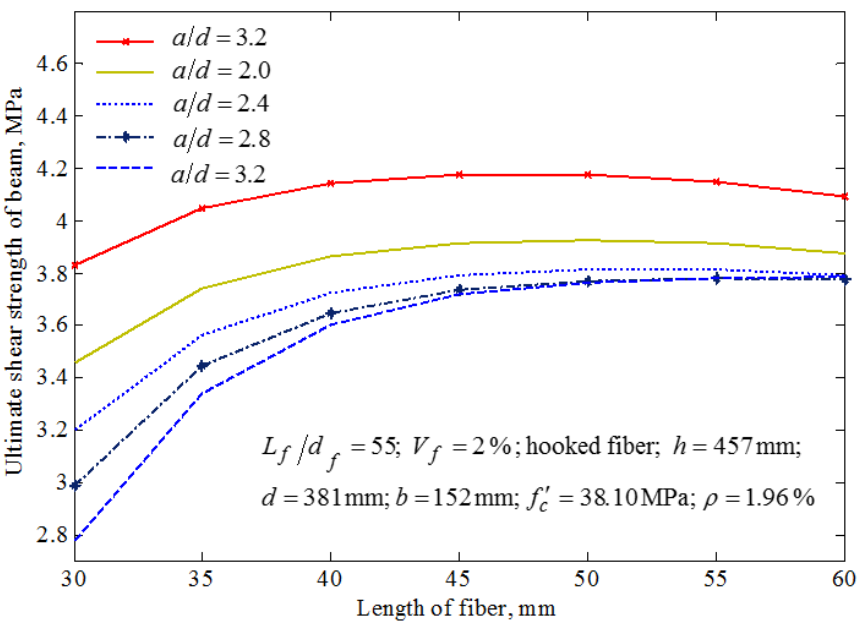

Figure 8: Influence length of fiber on the ultimate shear strength of SFRC beams without web reinforcement

7.2.4 Influence of Type of Fiber

Figure 9 shows the influence of the type of fiber on v_u of SFRC beams without web reinforcement for different a/d values. The properties of the studied SFRC beams are given in this figure. As can be seen from this figure for deep beams ($a/d<2$), all types of fiber have almost the same influence on v_u. However, for straight fibers, v_u is drastically decreased as the a/d increased for shallow beams ($a/d>2$). This demonstrated that straight fibers cannot be used as minimum web reinforcement for shallow beams.

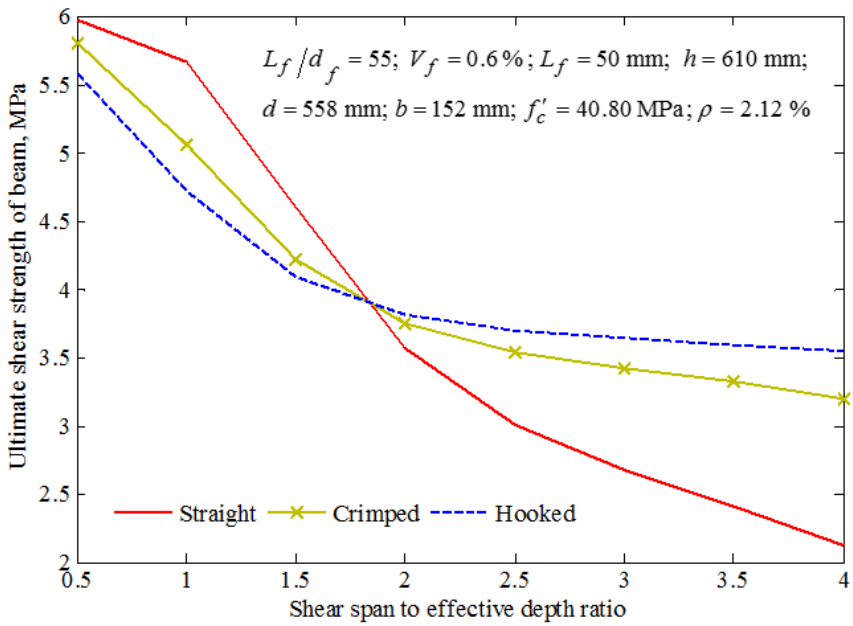

Figure 9: Influence type of fiber on the ultimate shear strength of SFRC beams without web reinforcement

8 CONCLUSIONS

Various researchers have developed regression analysis-based models for the prediction of the ultimate shear strength of SFRC beams. However, none of these models can perfectly predict the ultimate shear strength of SFRC beams. ANNs have been utilized in various fields including civil engineering to correlate the outputs and inputs of highly nonlinear problems. Nevertheless, very little research has been undertaken on the potential of using ANNs for the prediction of the ultimate shear strength of SFRC beams. This study is aimed at to develop a rational numerical model for the prediction of the ultimate shear strength of SFRC beams. From this study, the following conclusions were drawn:

A multilayer feed forward neural network (ANN-10) with a back propagation training algorithm and 14-neurons of two hidden layers was developed to predict the ultimate shear strength of SFRC beams. Experimental data of 70 SFRC beams reported in the technical literature by 11 research groups were utilized to train and test the ANN-10. The input parameters of ANN-10 were: i) the

properties of fiber (type, volume content, aspect ratio and length), ii) the properties the section (Overall depth, width, and effective depth), and, iii) the properties of the beam (shear span-to-effective depth ratio, percentage of longitudinal reinforcement, and the cylindrical compressive strength of concrete). ANN-10 exhibited excellent predictive performance for the prediction for both the training and testing data sets with 1.002 average of the predicted to experimental values. The successful performance of ANN-10 has established the favorable potential of ANNs to simulate of the complex shear behavior of SFRC beams.

A significant increase in the ultimate shear strength occurs for deep SFRC beams with increasing the fiber content. However, little increase in the ultimate shear strength occurred for shallow beams. In addition, the inclusion of 0.5% or more volume of steel fibers to fabricate the SFRC deep beams altered its failure mode from brittle shear to ductile flexure. In this study, up to 32% improvement of the ultimate shear strength of SFRC beams was observed by increasing the aspect ratio of the fiber from 60 to 100. The strength improvement in the deep beams was more pronounced than in the shallow beams. By increasing the fiber length from 30mm to 60mm, a 5~20% increase in the ultimate shear strength of SFRC beams was observed. The fiber length influences the flexural strength of the SFRC beams more than its shear strength. Straight, crimped and hooked fibers have almost a similar influence on the shear strength of SFRC beams for deep beams. However, the straight rounded fibers have very little influence on the ultimate shear strength of shallow beams.

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