

Degradation of the compressive strength of unstiffened/stiffened steel plates due to both-sides randomly distributed corrosion wastage

Abstract

The paper addresses the problem of the influence of randomly distributed corrosion wastage on the collapse strength and behaviour of unstiffened/stiffened steel plates in longitudinal compression. A series of elastic-plastic large deflection finite element analyses is performed on both-sides randomly corroded steel plates and stiffened plates. The effects of general corrosion are introduced into the finite element models using a novel random thickness surface model. Buckling strength, post-buckling behaviour, ultimate strength and post-ultimate behaviour of the models are investigated as results of both-sides random corrosion.

Keywords

imperfection, steel, plate, stiffener, both-sides corrosion, random thickness surface model, ultimate strength, buckling strength, behaviour, nonlinear finite element analysis.

Zorareh Hadj Mohammad
Esmail Nouri^a, Mohammad
Reza Khedmati^{*,b} and
Mohammad Mahdi Roshanali^c

^aPhD Candidate, Faculty of Marine Technology, Amirkabir University of Technology, Tehran 15914 – Iran

^bAssociate Professor, Faculty of Marine Technology, Amirkabir University of Technology, Tehran 15914 – Iran

^cMSc Student, Faculty of Marine Technology, Amirkabir University of Technology, Tehran 15914 – Iran

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* Author email: khedmati@aut.ac.ir

1 INTRODUCTION

Plates and stiffened plates are the most important load-carrying elements in thin-walled structures, such as ships and offshore platforms. In-plane compressive loads are approximately the most severe loads applied on such elements. Strength of plate and stiffened plate elements is crucial for the overall structural capacity of the whole structure.

On the other hand, ships and offshore platforms are operating in an aggressive maritime environment. As a result of interactions between metallic structures of ships and offshore platforms with the maritime environment, corrosion happens. Besides, corrosion may be considered as the undesirable deterioration of such structures in reacting with their surrounding environment. Corrosion has a harmful consequence from the view point of safety and can lead to thickness penetration, fatigue cracks, brittle fracture and unstable failure. These failures can imply a risk of loss of human lives and a risk of polluting the environment depending on the types of ships and offshore platforms.

NOTATION

AR	Aspect ratio of the plate
A_{0mn}	Coefficients in initial deflection function
A_p	Cross-sectional area of plate
A_s	Cross-sectional area of stiffener
a	Plate length
b	Plate breadth
b_f	Breadth of stiffener flange in un-corroded condition
d_w	Uniform reduction in thickness
E	Young modulus of material
h_w	Height of stiffener web in un-corroded condition
I	Moment of inertia
L	Span of stiffener
m	Number of half-waves in longitudinal direction
n	Number of half-waves in transverse direction
n_y	Number of years of exposure
P_u	Ultimate load
q	Weight per length
r_1, r_2	Random numbers corresponding to the corroded surfaces
S	Standard deviation of random thickness variations
t	Thickness in un-corroded condition
t_k	Thickness reduction due to corrosion
t_P	Thickness function
t_w	Thickness of stiffener web in un-corroded condition
t_f	Thickness of stiffener flange in un-corroded condition
U_x	Displacement along X-axis
U_y	Displacement along Y-axis
U_z	Displacement along Z-axis
ν	Poisson's ratio of material
W_0	Initial deflection function of plate
W_{0max}	Maximum magnitude of initial deflection of plate
W_s	Initial deflection function of stiffener
Z	Section modulus
z_{UpSRF}	Z-coordinate of the upper surface of the plate
z_{LowSRF}	Z-coordinate of the lower surface of the plate
β	Plate slenderness
μ	Mean corrosion depth
ε	Strain
ε_Y	Material yield strain
σ	Stress
σ_Y	Material yield stress
σ_{Ys}	Stiffener material yield stress
σ_{Yp}	Plate material yield stress
σ_{Cr}	Buckling strength
σ_U	Material ultimate stress
σ_{Ult}	Ultimate strength
φ_0	Angle of distortion of stiffener

Corrosion in marine structures is mainly observed in two distinct types, namely, general corrosion and localised corrosion. As an example of localised corrosion, reference may be made to the corrosion of hold frames in way of cargo holds of bulk carriers which have coating such as tar epoxy paints, Fig. 1 [10]. Generally, pitting corrosion is defined as an extremely localised corrosive attack and sites of the corrosive attack are relatively small compared to the overall exposed surface [3]. In the case of localised corrosion observed on hold frames of bulk carriers, the sites of the corrosive attack, that is, pits are relatively large (up to about 50mm in diameter).

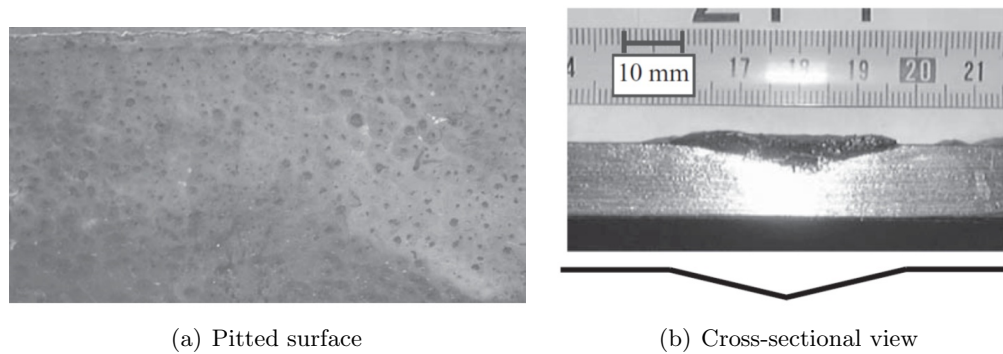


Figure 1 Pitted web plate of the hold frame of a bulk carrier [10].

General corrosion is the problem when the plate elements such as the hold frames of bulk carriers have no protective coating, Fig. 2. Both surfaces of the plate may be corroded, in a pattern like the sea waves spectrum, as shown in Fig. 2.

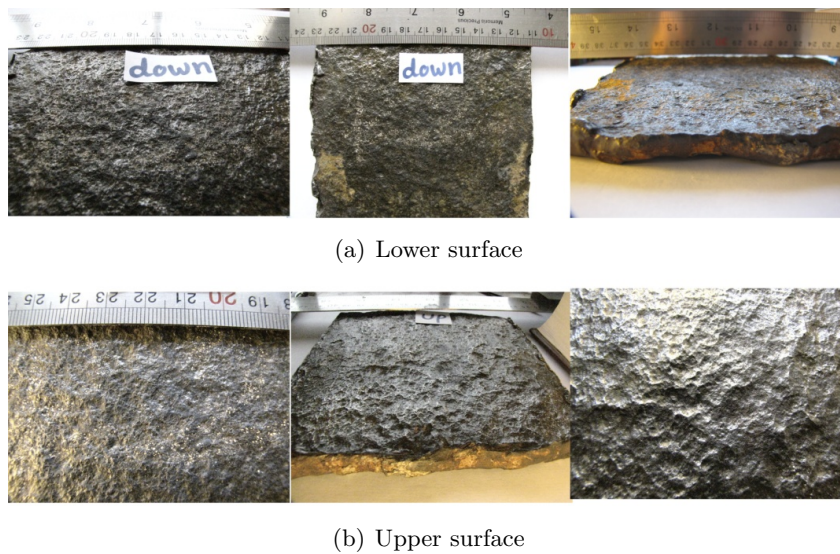


Figure 2 Plate with general corrosion.

2 RESEARCH BACKGROUND ON THE STRENGTH OF CORRODED PLATED ELEMENTS

The problem of strength analysis of plates and stiffened plates incorporating different corrosion types has attracted the attention of some researchers. History tree of key research studies on the strength of corroded plates and stiffened plates is prepared and shown in the Fig. 3. Of course, there may be some other research works relevant to the subject of investigating the strength of corroded plates and stiffened plates. However, a set of research reports and investigations, that have been available to the authors, is reviewed herein.

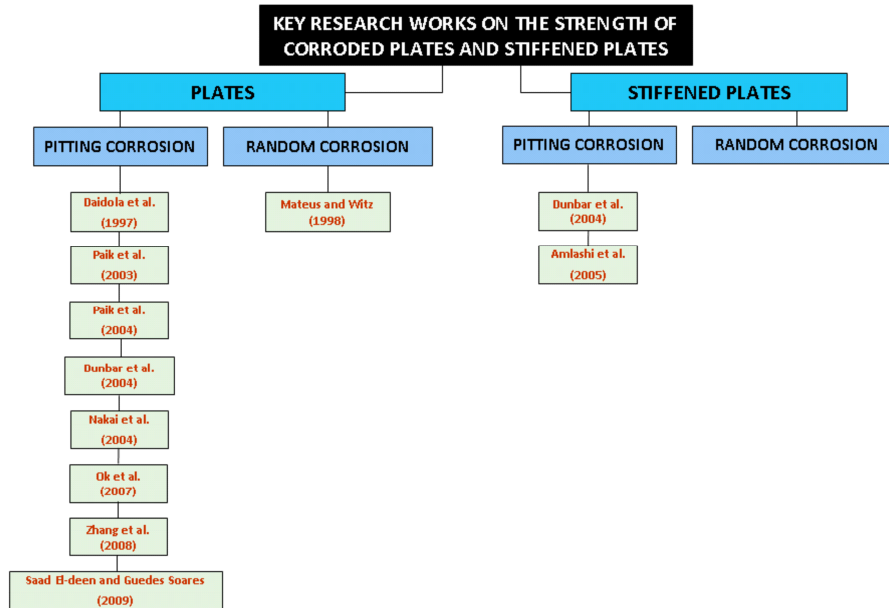


Figure 3 History tree of key research studies on the strength of corroded plates and stiffened plates.

2.1 Pitted plates

Daidola et al. [4] proposed a mathematical model to estimate the residual thickness of pitted plates using the average and maximum values of pitting data or the number of pits and the depth of the deepest pit, and presented a method to assess the effect of thickness reduction due to pitting on local yielding and plate buckling based on the probabilistic approach. Furthermore, they developed a set of tools which can be used to assess the residual strength of pitted plates.

Paik et al. [14, 15] studied the ultimate strength characteristics of pitted plate elements under axial compressive loads and in-plane shear loads, and derived closed form formulae for predicting the ultimate strength of pitted plates using the strength reduction (knock-down) factor approach. They dealt with the case where the shape of corrosion pits is a cylinder.

Dunbar et al. [5] investigated the effects of localised corrosion on the strength of plates. They applied finite element analyses in order to study initial buckling, ultimate collapse and

post-ultimate responses of the corroded plates.

Nakai and his collaborators [10, 11] performed a series of nonlinear finite-element (FE) analyses with pitted plates subjected to in-plane compressive loads and bending moments in order to investigate their behaviours. They also established a method for prediction of ultimate strength of plate models with pitted corrosion.

Ok et al. [13] focused on assessing the effects of localised pitting corrosion which concentrates at one or several possibly large area on the ultimate strength of unstiffened plates. They applied multi-variable regression method to derive new formulae to predict ultimate strength of unstiffened plates with localised corrosion. Their results indicated that the length, breadth and depth of pit corrosion have weakening effects on the ultimate strength of the plates while plate slenderness has only marginal effect on strength reduction. It was also revealed by them that transverse location of pit corrosion is an important factor determining the amount of strength reduction.

Zhang et al. [22] focused on the development of an assessing method for ultimate strength of ship hull plate with corrosion damnification. Pitting corrosion results in a quantity loss of the plate material as well as a significant degradation of the ultimate strength of the hull plate due to reducing of the effective thickness of the plate. Accordingly, the model for describing the correlations between the ultimate strength and the corroded volume loss of a corroded plate was proposed by them based on relative theory. Such model was then completed through numerical experiment by nonlinear finite element analyses for series of corroded plate models.

Later Saad Eldeen and Guedes Soares [16] investigated the collapse strength of pitted plates under in-plane compression. They performed some non-linear finite element analyses on the plates with different corrosion densities. Based on the obtained results, they could derive a formula in order to predict the ultimate strength reduction for the plates with pitting corrosion.

2.2 Pitted stiffened plates

Dunbar et al. [5], in some part of their research study, also investigated the collapse behaviour of stiffened plates under uni-axial compressive loads.

Besides, Amlashi and Moan [1] assessed the strength behaviour of stiffened plates under bi-axial compressive loading.

2.3 Randomly corroded plates

Mateus and Witz [9] investigated the effect of general corrosion on the post-buckling of plates using the uniform thickness reduction approach and a quasi-random thickness surface model. They revealed that the usual uniform thickness reduction approach to account for general corrosion effects is not adequate because plastic hinges formed due to plate surface irregularity slightly decreases its ultimate strength and significantly affects the post buckling behaviour of the plate.

2.4 Randomly corroded stiffened plates

To the knowledge of authors, there is not any key research work investigating the strength and collapse behaviour of stiffened plates.

The main objective of the present paper is to examine how general corrosion affects basic mechanical properties of plates and stiffened plates under compression and to explore the method of simulating behaviour of plated members with general corrosion by FE-analysis using shell elements. This paper presents the results of an investigation into the post-buckling behaviour and ultimate strength of imperfect corroded steel plates and stiffened plates used in ship and other related marine structures. A series of elastic-plastic large deflection finite element analyses is performed on both-sides randomly corroded steel plates and stiffened plates. The effects of general corrosion are introduced into the finite element models using a random thickness surface model. The effects on buckling and ultimate strengths as a result of parametric variation of the corrosion age are evaluated.

3 DESCRIPTION OF STRUCTURAL MODELS

3.1 Extent of the models and their characteristics

The plates in marine structures are of continuous nature. They are stiffened with longitudinal stiffeners and transverse frames. Longitudinal stiffeners and transverse frames divide the surface of the plates into isolated regions, Fig. 4(a). The filled region in Fig. 4(a) exhibits typically the extent of the plate models considered in the present investigation.

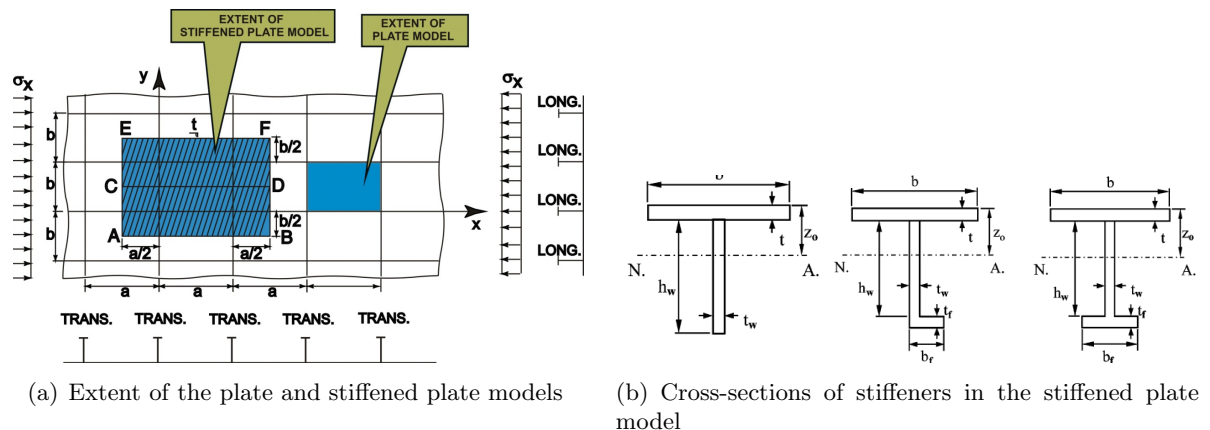


Figure 4 Extent of the models and their characteristics.

A triple span- triple bay (TS-TB) model (region ABFE in Fig. 4 (a)) has been chosen for the analysis of buckling/plastic collapse behaviour of corroded stiffened plates with symmetrical/unsymmetrical stiffeners [20]. This is the most complete and precise extent of the stiffened plate models when analysing their behaviour [20].

The geometrical characteristics of the analysed stiffened plates are given in Table 1. Three

types of models have been considered. In each type, three different shapes of stiffeners (Flat, Angle and Tee) have been attached to the isotropic plate, Fig. 4(b). The stiffeners of each type have the same moment of inertia. Types 1, 2 and 3 correspond respectively to weak, medium and heavy stiffeners.

In all analysed cases, local plate panels have a length of 2400 mm and a breadth of 800 mm.

Table 1 Geometrical characteristics of the analysed models of stiffened plates.

Type	Model	Shape	h_w	t_w	b_f	t_f	$I[\text{cm}^4]$	$q [\text{kg/m}]^*$	$Z_{\min} [\text{cm}^3]^*$
1	F1	flat	177	14	-	-	647	101.1	149
1	T1	tee	150	9	90	12	648	100.7	213
1	A1	angle	150	9	90	12	648	100.7	213
2	F2	flat	270	17	-	-	2,788	117.7	394
2	T2	tee	250	10	90	15	2,844	111.9	526
2	A2	angle	250	10	90	15	2,844	111.9	526
3	F3	flat	445	16	-	-	11,749	137.5	947
3	T3	tee	400	12	100	17	11,860	132.7	1,211
3	A3	angle	400	12	100	17	11,860	132.7	1,211

* Z_{\min} includes width 800 mm of the plate having thickness of 13 mm

3.2 Loading and boundary conditions

As shown in Fig. 4(a), each region of the continuous plate is surrounded by longitudinal stiffeners and transverse frames. To consider the effects of longitudinal stiffeners and transverse frames in the model of isolated plates, proper boundary conditions are to be applied on it. Description of applied boundary conditions in the plate models is shown in Fig. 5(a).

On the other hand, the boundary conditions of the analysed stiffened plates are as follow:

- In the case of unsymmetrical stiffeners, periodically continuous conditions are imposed at the same x-coordinate along the longitudinal edges (i.e. along AB and EF). These conditions are defined as below:

$$\begin{aligned}
 u_{AB} &= u_{EF} \\
 w_{AB} &= w_{EF} \\
 \theta_{x-AB} &= \theta_{x-EF} \\
 \theta_{y-AB} &= \theta_{y-EF} \\
 \theta_{z-AB} &= \theta_{z-EF}
 \end{aligned} \tag{1}$$

- In the case of symmetrical stiffeners, symmetry conditions are imposed at the same x-coordinate along the longitudinal edges (i.e. along AB and EF).

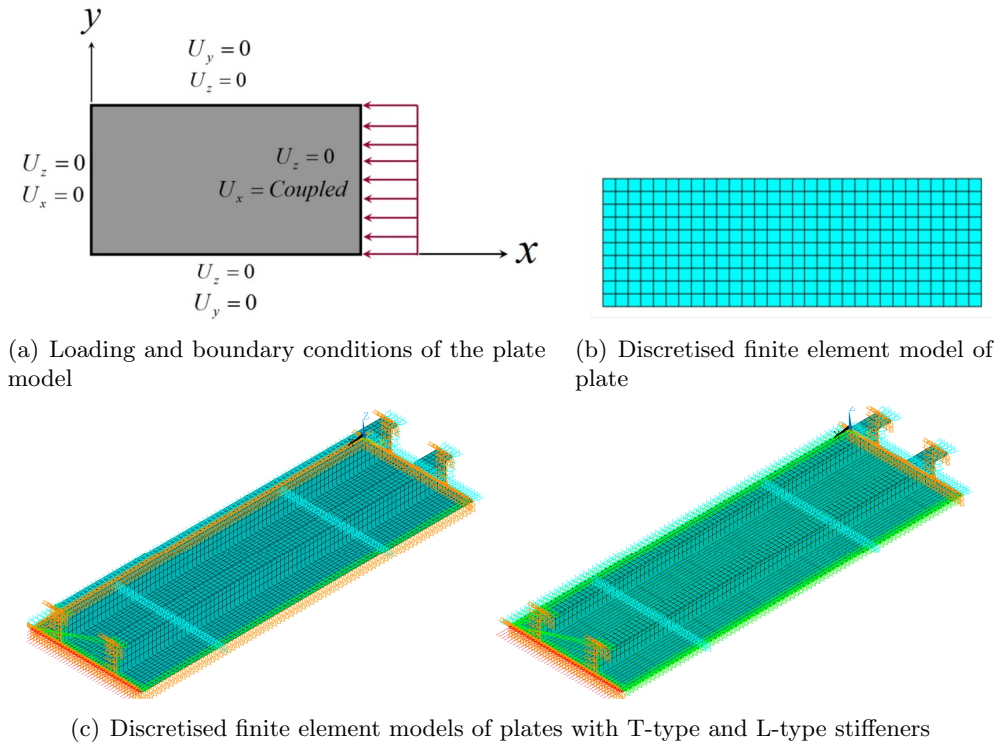


Figure 5 Loading and boundary conditions.

- When the aspect ratio of the local plate panels is an even or odd number, then periodically continuous conditions or symmetry conditions are imposed respectively at the same y -coordinate along the transverse edges in the model (i.e. along AE and BF).
- Although transverse frames are not modelled, the out-of-plane deformation of plate is restrained along its junction line with the transverse frame.
- To consider the plate continuity, in-plane movement of the plate edges in their perpendicular directions is assumed to be uniform.

Loading would be compressive along x -axis of the Fig. 4(a). The uniaxial compressive loading was applied by controlled edge displacement.

3.3 Finite Element code, adopted element and mesh density

A non-linear elastic-plastic finite element analysis is the only method capable of simulating the succession of all phenomena that occur during the quasi-static compression of a plate or a stiffened plate. To predict the ultimate strength of thin-walled plated structures, plate-shell elements are employed for both membrane and bending stiffness. In this analysis the mesh size must be fine enough to capture the long-wave-length buckling modes, such as torsional

buckling, and also to account for the continuity of the plate through the transverse frames. Furthermore, the mesh needs to be fine enough to recognize the initial imperfections to make sure that buckling occurs and to avoid unduly stiff behaviour. The buckling/plastic collapse behaviour and ultimate strength of models are hereby assessed using ANSYS [2], in which both material and geometric nonlinearities are taken into account. An APDL code was prepared inside ANSYS environment to facilitate parametric modelling and analysis using ANSYS [2].

Plates and stiffeners are modelled by SHELL181 elements with elastic-plastic large deflection solution option. SHELL181 is suitable for analyzing thin to moderately-thick shell structures. It is a 4-node element with six degrees of freedom at each node: translations in the x, y, and z directions, and rotations about the x, y, and z-axes. SHELL181 is well-suited for linear, large rotation, and/or large strain nonlinear applications. Change in shell thickness is accounted for in nonlinear analyses. In order to obtain reasonable results a number of sensitivity analyses were carried out to find out the optimum mesh density and proper values of nonlinear analysis options. Samples of finite element discretisations are represented in Figs. 5(b) and 5(c).

3.4 Applied material properties

The material used in the models was of normal strength steel (abbreviated by NS steel) type. This type of steel has Young's modulus of 21000 kgf/mm^2 and Poisson's ratio of 0.3. The yield strength of 24 kgf/mm^2 is taken into account for NS steel.

It is evident that strain-hardening effect has some influence on the nonlinear behaviour of plates. The degree of such an influence is a function of many factors including plate slenderness. In this study, material behaviour for plate was modelled as a bi-linear elastic-plastic manner with strain-hardening rate of $E/65$, Fig. 6. This value of strain-hardening rate was obtained through a large number of elastic-plastic large deflection analyses made by Khedmati [8].

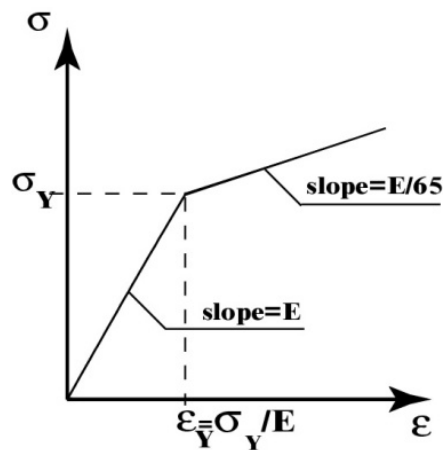


Figure 6 Idealised bilinear model for material stress-strain curve.

3.5 Initial deflections in plate and stiffener

The actual mode of the initial deflection of the plate is very complex, Fig. 7 [6, 7]. This complex mode can be expressed by a double sinusoidal series as:

$$w_0 = \sum_{m=1}^{\infty} \sum_{n=1}^{\infty} A_{0mn} \sin \frac{m\pi x}{a} \sin \frac{n\pi y}{b} \quad (2)$$

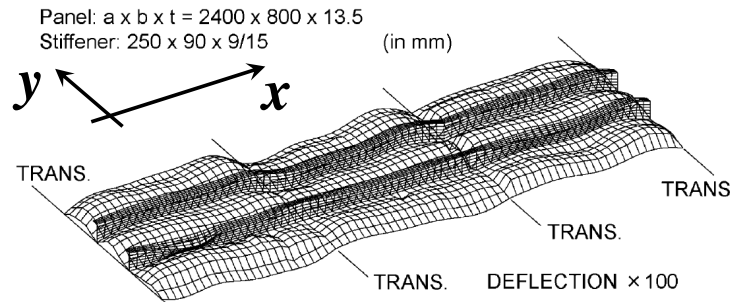


Figure 7 Real distribution of initial deflection or so-called thin-horse mode initial deflection [6, 7].

When compressive load acts in the direction of the longer side of the plate (x-direction), the deflection components in the direction of the shorter side of the plate (y-direction) decrease with the increase in load except the first term with one half-wave. In this case, only the first term ($n = 1$) may play a dominant role, and the simpler form of initial deflection can be used for analysis as follows:

$$w_0 = \sum_{m=1}^{\infty} A_{0m1} \sin \frac{m\pi x}{a} \sin \frac{\pi y}{b} \quad (3)$$

Ueda and Yao [19] used only odd terms. Finally Yao et. al. [21] introduced even terms also in this mode, and the so-called “*idealized thin-horse mode*” took the following form:

$$w_0 = \sum_{m=1}^{11} A_{0m1} \sin \frac{m\pi x}{a} \sin \frac{\pi y}{b} \quad (4)$$

The coefficients of this mode are given in Table 2 [21] as functions of plate aspect ratio and its thickness. The coefficients are so scaled that the maximum magnitude of initial deflection, $w_{0\max}$, is to be as:

$$w_{0\max} = 0.05\beta^2 t \quad (5)$$

Where β is the slenderness parameter of the plate and defined by:

$$\beta = \frac{b}{t} \sqrt{\frac{\sigma_Y}{E}} \quad (6)$$

where σ_Y and E are yield stress and modulus of elasticity of the plate, respectively.

Table 2 Coefficients of thin-horse mode initial deflection as a function of plate aspect ratio [21].

a/b	A01/t	A02/t	A03/t	A04/t	A05/t	A06/t
$1 < a/b < \sqrt{2}$	1.1158	-0.0276	0.1377	0.0025	-0.0123	-0.0009
$\sqrt{2} < a/b < \sqrt{6}$	1.1421	-0.0457	0.2284	0.0065	0.0326	-0.0022
$\sqrt{6} < a/b < \sqrt{12}$	1.1458	-0.0616	0.3079	0.0229	0.1146	-0.0065
$\sqrt{12} < a/b < \sqrt{20}$	1.1439	-0.0677	0.3385	0.0316	0.1579	-0.0149
$\sqrt{20} < a/b < \sqrt{30}$	1.1271	-0.0697	0.3483	0.0375	0.1787	-0.0199

a/b	A07/t	A08/t	A09/t	A010/t	A011/t
$1 < a/b < \sqrt{2}$	-0.0043	0.0008	0.0039	-0.0002	-0.0011
$\sqrt{2} < a/b < \sqrt{6}$	-0.0109	0.001	-0.0049	-0.0005	0.0027
$\sqrt{6} < a/b < \sqrt{12}$	0.0327	0.000	0.000	-0.0015	-0.0074
$\sqrt{12} < a/b < \sqrt{20}$	0.0743	0.0059	0.0293	-0.0012	0.0062
$\sqrt{20} < a/b < \sqrt{30}$	0.0995	0.0107	0.0537	-0.0051	0.0256

The following initial imperfections were accounted for in analysing the stiffened plate models in this study:

- Real distribution of initial deflection mode for the plate as explained by Eq. (4), as represented by Fig. 8(a). This is a distinction point between this study and other related studies which have been previously done on the strength of corroded plates and stiffened plates. Mateus and Witz [9] assumed the following single-term expression for defining the initial deflection of the corroded plate based on simplified analyses made by Smith et al. [17]:

$$w_0 = 0.1\beta^2 t \sin \frac{\pi x}{a} \sin \frac{\pi y}{b} \tag{7}$$

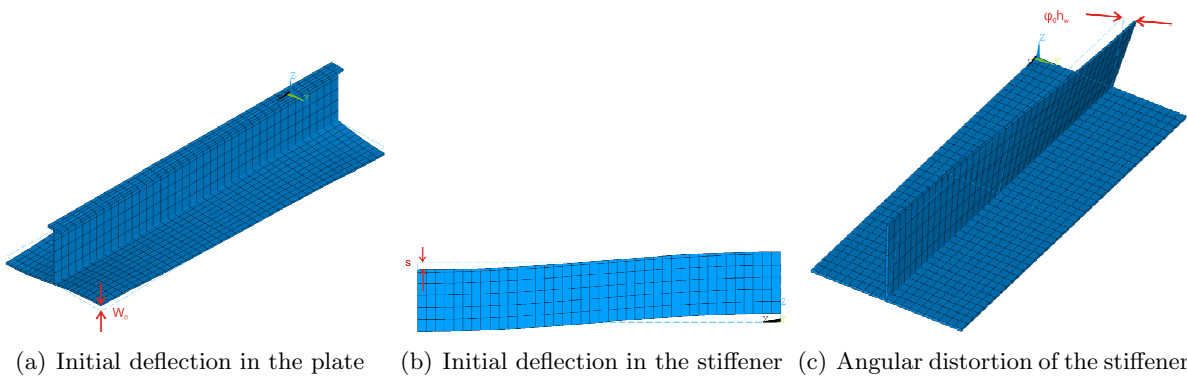


Figure 8 Components of initial imperfections in the stiffened plate models.

Besides, more or less the same single-term expression for initial plate deflection mode, as described by Eq. (7), was adopted in other researches on this topic. This is mainly due to ease of analyses using Eq. (7).

- Initial deflection for the stiffener as expressed by Eq. (8) and represented by Fig. 8(b)

$$w_s = (0.0025 \times a) \sin \frac{\pi x}{a} \quad (8)$$

- Angular distortion of the stiffener which is taken as (Fig. 8(c))

$$\varnothing_0 h_w = (0.0025 \times a) \sin \frac{\pi x}{a} \quad (9)$$

The authors prepared a computer code in FORTRAN90 language in order to produce the initial imperfections expressed by Eqs. (4), (8) and (9) inside the models.

3.6 Random general corrosion modelling

A plate/stiffened plate subject to general corrosion has a random distribution of thickness over its area. The likelihood of these variations in thickness to form plastic hinges that may affect the buckling and post-buckling behaviour of a corroded plate/stiffened plate, and perhaps its ultimate strength, is something that cannot be discarded without further analysis [9].

The extent of general corrosion in marine structures is reflected in the results published by Ohyagi [12] based on the compilation of data gathered by Nippon Kaiji Kyokai (NKK) from corrosion surveys on ships. He gave the mean and minimum values of thickness measured at each inspection and also other statistical parameters of significance such as the standard deviation. According to the results of the NKK surveys, general cargo carriers are most affected by corrosion and the cargo holds are the most corroded spaces.

Ohyagi's uniform thickness reduction general corrosion model has a mean linear trend for maximum corrosion rates. Besides, it is following a normal distribution for the probability of exceedance of corrosion rate and explained by [12]:

$$d_w = 0.34n_y \quad (10)$$

where n_y is the number of years of exposure and d_w is the uniform reduction in thickness in millimeters after n_y years of exposure. The standard deviation associated with the normal distribution is 0.23mm, based on the studies of Ohyagi [12].

It may be reasonable to assume that the corroded surfaces of a plate with its random thickness variation is composed of an infinite summation of random coefficients associated with each of the elastic buckling modes of the plate. In numerical terms the general corrosion model describes the typical surfaces of a corroded plate as a random thickness variation, t_p , with an average value equal to the original thickness of plate, minus the corroded equivalent thickness reduction. The following expression was applied in the studies made by Mateus and Witz [9]

$$t_p(x, y) = t - d_w + \sum_{i=1}^{\infty} \sum_{k=1}^{\infty} (A_i \cdot f_i(x) + B_k \cdot g_k(y)) \quad (11)$$

where A_i and B_k are the random coefficients associated with mode i in the x-direction and the mode k in the y-direction, respectively and $f_i = \sin(i\pi x/a)$, $g_k = \sin(k\pi y/b)$.

Establishment of proper values for A_i and B_k in Eq. (8) is not so easy to the researchers. That is why; instead of above-mentioned expression of double sinusoidal summation, a more practical way was adopted in this paper in order to generate randomly corroded surfaces for plates. A special purpose computer code was written in FORTRAN90 language. Generation of randomly corroded surfaces was achieved using the features of the GDIS function of FORTRAN90. The modified version of Eq. (11), which was developed and used in this research, can be expressed as:

$$t_p(x, y) = t - d_w + DRANDM(0) \quad (12)$$

There was one limitation in the generation process and it was standard deviation of the plate thicknesses at different nodes that was set to 0.23mm, as investigated by Ohyagi [12].

Different surfaces and relevant parameters corresponding to the case of a plate element with general corrosion are shown in Fig. 9(a). Definition of different layers in case of both-sides randomly distributed general corrosion is given in Fig. 9(b). Three different layers are considered through the thickness of each of the SHELL181 elements used for discretisation of the plate. The thickness of middle layer is equal to $(t - d_w)$, while the thicknesses of upper and lower layers are adjusted by random values of r_1 , r_2 .

Finally, z-coordinate of upper and lower surfaces of both-sides randomly corroded plate can be defined as:

$$z_{LowSRF} = w_0 - \frac{t - d_w}{2} - r_1 \quad , \quad z_{UpSRF} = w_0 + \frac{t - d_w}{2} + r_2 \quad (13)$$

where

$$t_p = z_{UpSRF} - z_{LowSRF} = t - d_w + r_1 + r_2 \quad (14)$$

Random values of r_1 and r_2 are produced by GDIS function.

The same procedure, as described above, was also applied to stiffener web and flange elements. Figures 9(c) and 9(d) exhibit respectively perspective views of typical both-sides randomly corroded plates and stiffened plates.

3.7 Validation

Tanaka & Endo [18] carried out a series of experimental and numerical investigations on the ultimate compressive strength of plates having three and two flat-bars stiffeners welded longitudinally and transversally respectively. A total of 12 tests were performed. The test specimen was designed so that the longitudinally stiffened plates located in the middle of whole test specimens could fail. The test specimens were intended to fail by local plate buckling or tripping of longitudinal stiffeners. A typical test rig from the Tanaka & Endo study is shown in Fig. 10. A stiffened plate model positioned in their testing rig is presented schematically in

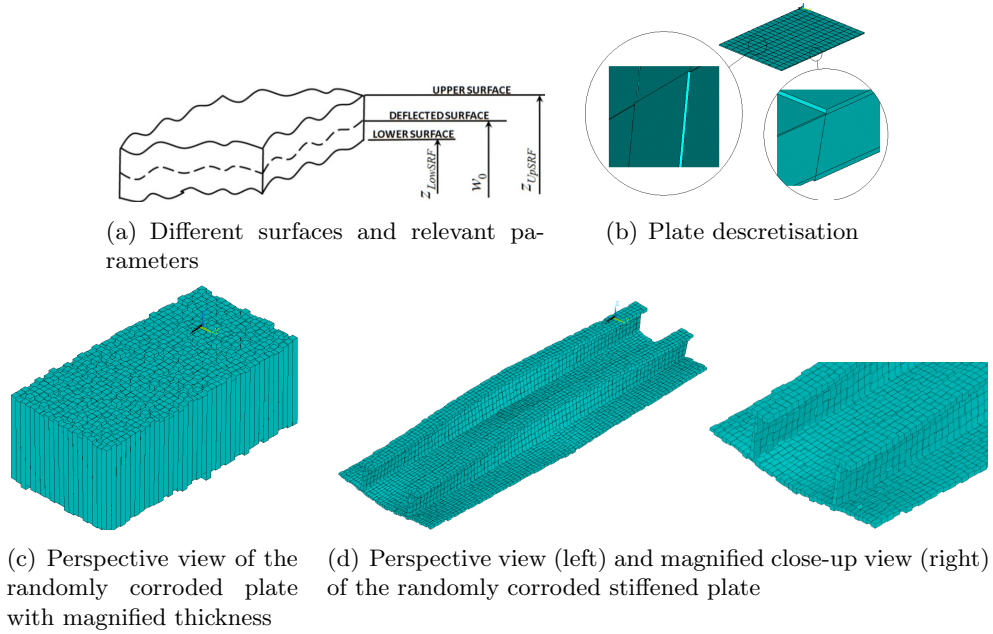


Figure 9 Finite element analysis modeling details for general corrosion.

Fig. 11. To account for the effect of adjacent panels on the collapse behaviour of central panel, three-span models with two adjacent (dummy) stiffened panels and supported by two transverse frames were employed. The thickness of plate and stiffeners in two adjacent panels was 1.2-1.3 times that of plate and stiffeners in the central panel. Table 3, where $L = 1080\text{mm}$ is the span length of the plate with average plate thickness between $t = 4.38\text{mm}$ to $t = 6.15\text{mm}$, represents geometric and material properties for the Tanaka & Endo test structures. The boundaries of stiffened plates were continuous simply supported and the in-plane axial compression load was applied longitudinally. The maximum measured initial deflections in the plate were ranging between 0.1-0.4 mm.

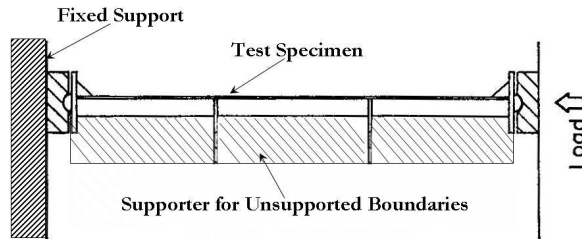


Figure 10 Stiffened plate model positioned in the Tanaka & Endo testing rig [18].

In each test the maximum collapse stress σ_{Ult} was calculated by dividing the ultimate load P_u to the overall cross-section of the plate A_p and stiffeners A_s as given by Eq. (15)

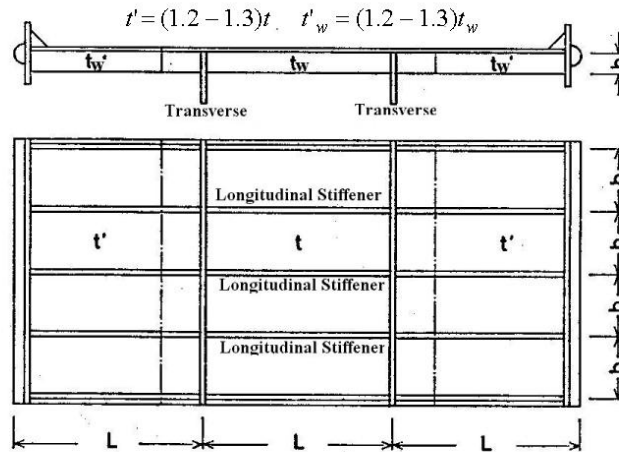


Figure 11 Tanaka & Endo test model [18].

Table 3 Geometric and material properties of Tanaka & Endo tests.

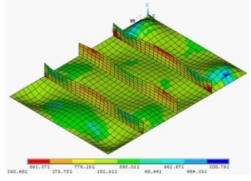
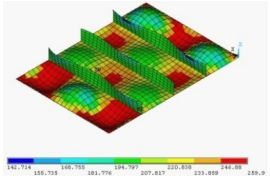
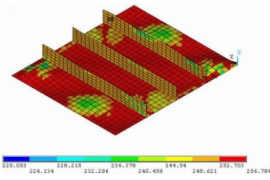
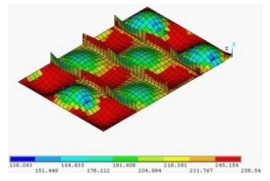
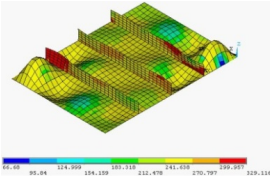
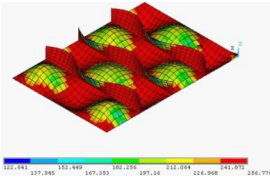
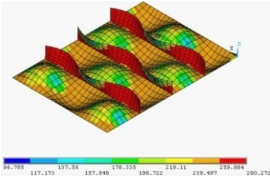
Structure No.	L (mm)	b (mm)	t (mm)	h_w (mm)	t_w (mm)	$\frac{h_w}{t_w}$	A_{03} (mm)	σ_{Yp} (MPa)	σ_{Ys} (MPa)	E (GPa)
D0		1440	6.15	110.0	9.77	11.26	0.101	234.2	287.1	205.8
D0A		1440	5.65	110.0	10.15	10.84	0.250	249.9	196.0	205.8
D1		1200	5.95	110.0	10.19	10.79	0.143	253.8	250.9	205.8
D2		1560	5.95	110.0	10.19	10.79	0.288	253.8	250.9	205.8
D3	1080	1440	5.95	103.5	11.84	8.74	0.312	253.8	326.3	205.8
D4		1440	5.95	118.5	7.98	14.85	0.119	253.8	284.2	205.8
D4A		1440	5.65	118.5	8.08	14.67	0.379	249.9	274.4	205.8
D10		1200	4.38	65.0	4.38	14.84	0.515	442.0	442.0	205.8
D11		1200	4.38	90.0	4.38	20.55	0.503	442.0	442.0	205.8
D12		1440	4.38	65.0	4.38	14.84	0.523	442.0	442.0	205.8

$$\sigma_{Ult} = P_u / (A_p + A_s) \tag{15}$$

A summary of the results obtained through the finite element simulation of the tests carried out by Tanaka & Endo is given in Table 4. Also, in these tables, the obtained collapse modes from FEM analyses are shown. Comparison of the results show that in general good agreement exists among the FEM results with those obtained from the tests.

In Tanaka & Endo tests, the longitudinally stiffened plate located in the middle of the whole test specimens were simulated assuming all edges, simply supported and straight. The same boundary conditions as those of Tanaka & Endo in their finite element simulation of their own test procedures were considered in this study, Fig. 12. In such cases, finite element simulation results, described also well the interactive buckling of plates and stiffeners in most of the cases, (Table 4). The smallest value of stiffener web height-to-web thickness ratio belongs to model D3, while the biggest value of this ratio corresponds to models D4 and D4A. Model D3 has failed due to local deformation in the plate, while in the case of models D4 and D4A the collapse has been produced by large plastic deformations both in the plate and stiffeners.

Table 4 Summary of results for some of Tanaka & Endo tests.

Structure No.	Tanaka & Endo		Present Collapse mode
	$\frac{(\sigma_{Ult})_{FEM}}{(\sigma_{Ult})_{EXPERIMENT}}$	$\frac{(\sigma_{Ult})_{FEM}}{(\sigma_{Ult})_{EXPERIMENT}}$	
D0	0.977	1.014	
D0A	1.028	1.065	
D1	0.869	0.911	
D2	0.936	0.944	
D3	0.860	0.853	
D4	0.792	0.866	
D4A	0.866	0.960	

Interactive buckling in both plate and stiffeners can be observed in other models, where the level of plastic deformations, in the plate varies among them. The values of the ultimate strength predicted by FEM in this work are in better consistency as compared with those obtained by Tanaka & Endo [18]. The reason may be due to the fact that in such cases, the initial deflection of the test specimens was simulated in FEM with a better accuracy.

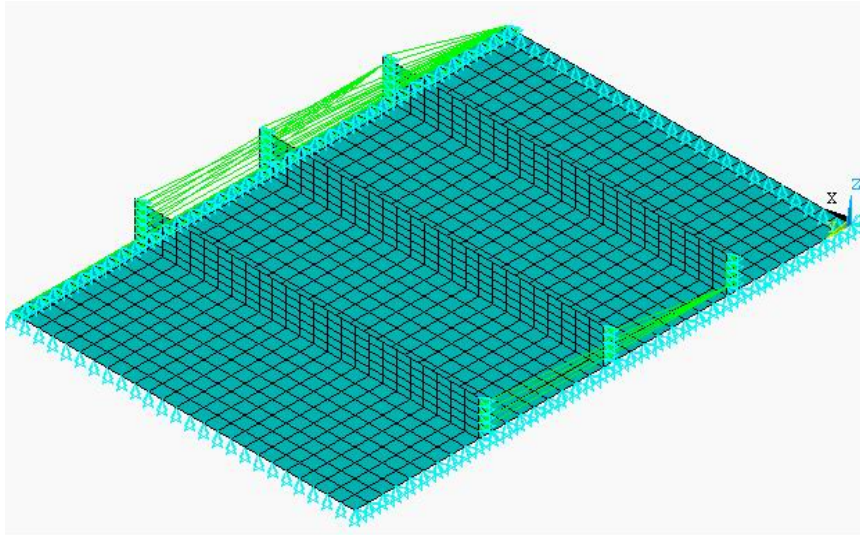


Figure 12 Finite element model of Tanaka & Endo test specimens.

4 INVESTIGATED PARAMETRIC MODELS

4.1 Plate models

In order to study the effects of random thickness variation on the response of axially loaded plates, different cases were considered. The cases included in the study are briefly explained in the following

- Corroded plates with $AR=2$, $t=10-20$ mm and $S = 0.23$ made of NS steel
- Corroded plates with $AR=3$, $t=10-20$ mm and $S = 0.23$ made of NS steel

4.2 Stiffened plate models

Besides, in order to study the effects of random thickness variation on the response of axially loaded stiffened plates, the following cases were generated and considered

- Plate aspect ratio: $AR = 3$
- Plate original thickness in un-corroded condition: $t = 13$ mm

- Stiffener type, shape and size: $F1, F2, F3, T1, T2, T3, L1, L2, L3$
- Mean corrosion depth: $\mu = 2\text{mm}$
- Standard deviation of random thickness variations: $S = 0.2, 0.4 \text{ mm}$
- Material: NS steel

5 RESULTS AND DISCUSSIONS

5.1 Plate models

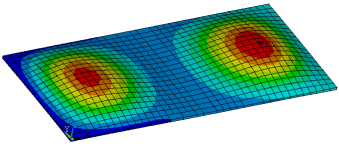
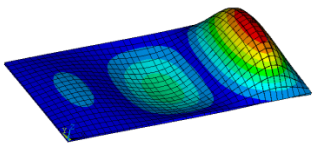
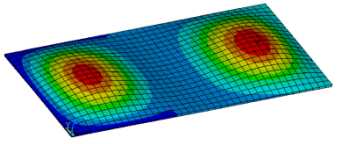
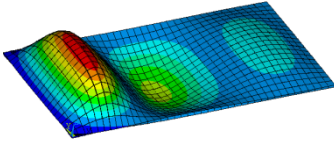
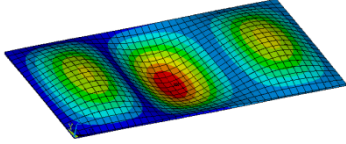
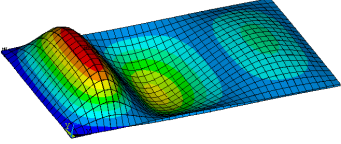
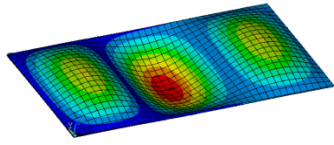
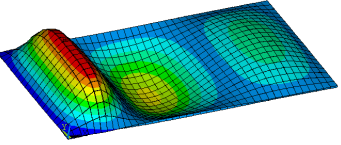
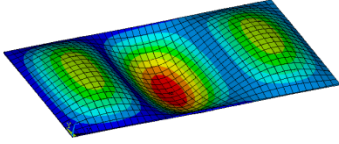
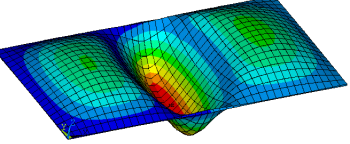
For each of above cases, different models were created changing the age of the plate. The ages considered for the models were 5, 10, 15 and 20 years of exposure to the sea water. The corroded surfaces of the models were different in these cases. All of the plate models were analysed under longitudinal in-plane compression. Average stress-average strain relationships for the models are shown respectively in the Figs. 13 to 18. The maximum magnitude of thin-horse mode initial deflection for the corroded models is calculated using the Eq. (5) for the original thickness. Also, Von Mises stress distributions are shown for a selection of the cases representing thin and thick plates in Tables 5, 6, 7 and 8. On the other hand, Tables 9, 10, 11 and 12 give a summary of results regarding degradation of the buckling/ultimate strength as results of corrosion of the plate.

The average stress-average strain relationships of the plate models in un-corroded condition are shown in the Figs 13 to 16 for selected thin and thick plates.

Figures 13 to 18 in addition to the results summarised in Tables 5 to 12 reveal the following main characteristics for the buckling/ultimate strengths and behaviours of the corroded plate models.

- Age or sea exposure life of the plate models affects mainly their post-buckling-strength regimes and degrades their buckling/ultimate strength.
- Average stress-average strain relationships of the thin plates at lower exposure times and also those of the thick plates at upper exposure times show snap-back behaviours of the plate (Figs. 13, 17, 18 and also table 5). This is mainly due to the very thin plate of both-sides randomly corroded plate. The ultimate strength or collapse mode of the plate of aspect ratio equal to 2 with the original un-corroded thickness of 14 mm exhibit creation of three buckling half-waves as a result of snap-back behaviours described above.
- Thin plates at all ages and also thick plates at upper exposure time show that they undergo elastic buckling with distinct distance between the buckling and ultimate strength levels, Figs. 13 to 18.
- Figures 13, 15 and 17 reveals the fact that for the thin/thick plates having the aspect ratio of 2, beside decrease in the ultimate strength as a direct function of the age of the plate, the ultimate strain is also diminished. On the contrary, when the aspect ratio of

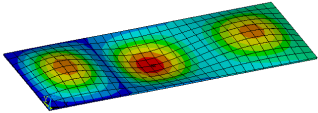
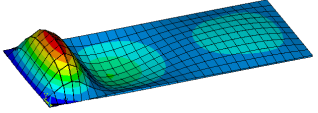
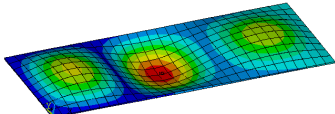
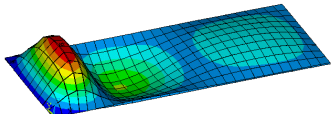
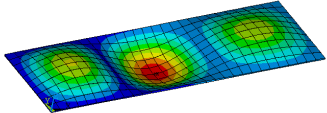
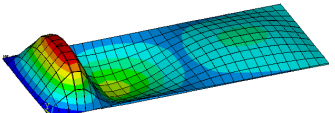
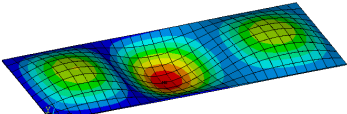
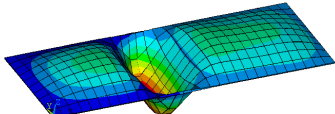
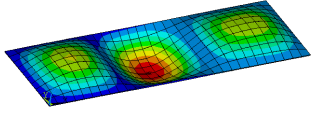
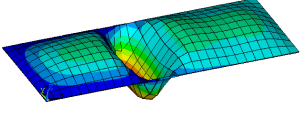
Table 5 Deformation mode and spread of plasticity for the plate of dimensions 1600×800×14 mm (AR=2) with 5-20 years exposure (magnification factor for deformation mode: 10).

Case	Ultimate strength level	Final step
Uncorroded $t = 14$ mm		
5-year $t = 13.17$ mm		
10-year $t = 11.73$ mm		
15-year $t = 9.94$ mm		
20-year $t = 8.18$ mm		

thin/thick plate is 3, the ultimate strain remains almost unchanged while the ultimate strength decreases as a direct function of exposure time, Figs. 14, 16 and 18. Thus, one of the main factors influencing the ultimate strength of the corroded steel plates would be their aspect ratio.

- The post-ultimate-strength regimes of the corroded thin/thick plate show a uniform reduction in the reserve strength of the plate as its exposure time increases, Figs. 13 to 16.
- The mode shapes and Von Mises stress contours shown in Tables 5 to 8 reveal that

Table 6 Deformation mode and spread of plasticity for the plate of dimensions 2400×800×14 mm (AR=3) with 5-20 years exposure (magnification factor for deformation mode: 10).

Case	Ultimate strength level	Final step
Uncorroded $t = 14$ mm		
5-year $t = 13.3$ mm		
10-year $t = 11.75$ mm		
15-year $t = 10.04$ mm		
20-year $t = 8.23$ mm		

almost regular half-waves are generated inside the plate extent in longitudinal direction at the ultimate strength level. Besides, post-ultimate-strength mode shapes show the local accumulation of deflection in some regions of the plate model in addition to the unloading the rest of plate area. The place of local deflection accumulation is not fixed and in other words changed from case to case.

- Tables 9 to 12 represent the degradation percentages of the buckling and ultimate strengths of the corroded plates. The difference values are defined as follows

$$\begin{cases} (\Delta\sigma)_{Cr} = \frac{(\sigma_{Cr})_{Uncorroded} - (\sigma_{Cr})_{Corroded}}{(\sigma_{Cr})_{Uncorroded}} \times 100 \\ (\Delta\sigma)_{Ult} = \frac{(\sigma_{Ult})_{Uncorroded} - (\sigma_{Ult})_{Corroded}}{(\sigma_{Ult})_{Uncorroded}} \times 100 \end{cases} \quad (16)$$

Table 7 Deformation mode and spread of plasticity for the plate of dimensions 1600×800×18 mm (AR=2) with 5-20 years exposure (magnification factor for deformation mode: 10).

Case	Ultimate strength level	Final step
Uncorroded $t = 18 \text{ mm}$		
5-year $t = 17.47 \text{ mm}$		
10-year $t = 15.50 \text{ mm}$		
15-year $t = 13.79 \text{ mm}$		
20-year $t = 12.43 \text{ mm}$		

Buckling strength reduction is about 40 to 70 percents for the plates at 20 years of exposure to sea water, depending on the plate aspect ratio and slenderness parameter. This is while the ultimate strength diminishes about 27-40 percents at the age of 20 for both-sides randomly corroded steel plates depending on their afore-mentioned parameters.

Table 8 Deformation mode and spread of plasticity for the plate of dimensions 2400×800×18 mm (AR=3) with 5-20 years exposure (magnification factor for deformation mode: 10).

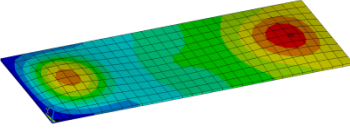
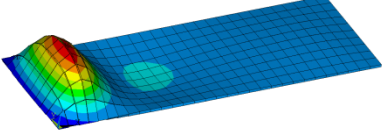
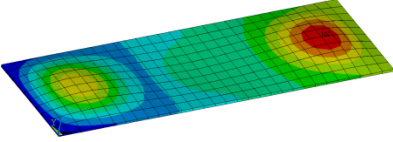
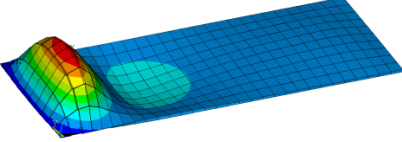
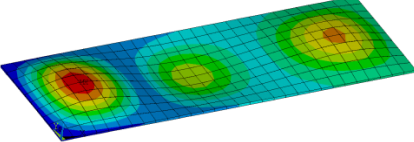
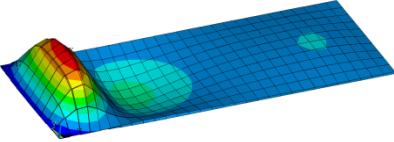
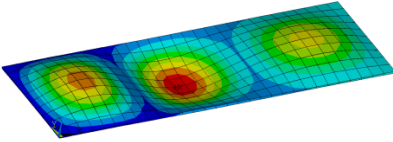
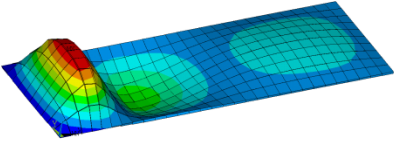
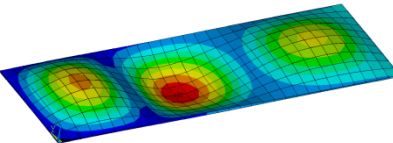
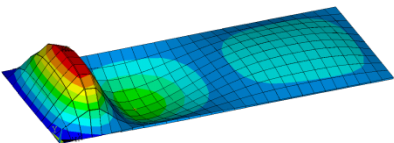
Case	Ultimate strength level	Final step
Uncorroded $t = 18$ mm		
5-year $t = 17.47$ mm		
10-year $t = 15.50$ mm		
15-year $t = 13.79$ mm		
20-year $t = 12.43$ mm		

Table 9 Comparison of results for plate 1600×800×14 mm with 0-20 years of exposure.

Case	Buckling Strength		Ultimate Strength	
	$\frac{\sigma_{Cr}}{\sigma_{Yp}}$	$(\Delta\sigma)_{Cr}$	$\frac{\sigma_{Ult}}{\sigma_{Yp}}$	$(\Delta\sigma)_{Ult}$
uncorroded	0.643	0	0.772	0
5-year exposure	0.596	7.39	0.724	6.21
10-year exposure	0.471	26.68	0.601	22.15
15-year exposure	0.280	56.45	0.535	30.67
20-year exposure	0.204	68.20	0.476	38.39

Table 10 Comparison of results for plate 2400×800×14 mm with 0-20 years of exposure.

Case	Buckling Strength		Ultimate Strength	
	$\frac{\sigma_{Cr}}{\sigma_{Yp}}$	$(\Delta\sigma)_{Cr}$	$\frac{\sigma_{Ult}}{\sigma_{Yp}}$	$(\Delta\sigma)_{Ult}$
uncorroded	0.661	0	0.750	0
5-year exposure	0.602	8.99	0.701	6.46
10-year exposure	0.472	28.67	0.634	15.49
15-year exposure	0.348	47.38	0.575	23.27
20-year exposure	0.253	61.67	0.531	29.22

Table 11 Comparison of results for plate 1600×800×18 mm with 0-20 years of exposure.

Case	Buckling Strength		Ultimate Strength	
	$\frac{\sigma_{Cr}}{\sigma_{Yp}}$	$(\Delta\sigma)_{Cr}$	$\frac{\sigma_{Ult}}{\sigma_{Yp}}$	$(\Delta\sigma)_{Ult}$
uncorroded	0.889	0	0.931	0
5-year exposure	0.8229	7.50	0.885	4.91
10-year exposure	0.7769	12.66	0.841	9.62
15-year exposure	0.617	30.60	0.760	18.34
20-year exposure	0.475	46.50	0.632	32.13

Table 12 Comparison of results for plate 2400×800×18 mm with 0-20 years of exposure.

Case	Buckling Strength		Ultimate Strength	
	$\frac{\sigma_{Cr}}{\sigma_{Yp}}$	$(\Delta\sigma)_{Cr}$	$\frac{\sigma_{Ult}}{\sigma_{Yp}}$	$(\Delta\sigma)_{Ult}$
uncorroded	0.872	0	0.924	0
5-year exposure	0.811	6.94	0.887	3.93
10-year exposure	0.745	14.56	0.814	11.89
15-year exposure	0.616	29.38	0.724	21.58
20-year exposure	0.511	41.38	0.661	28.47

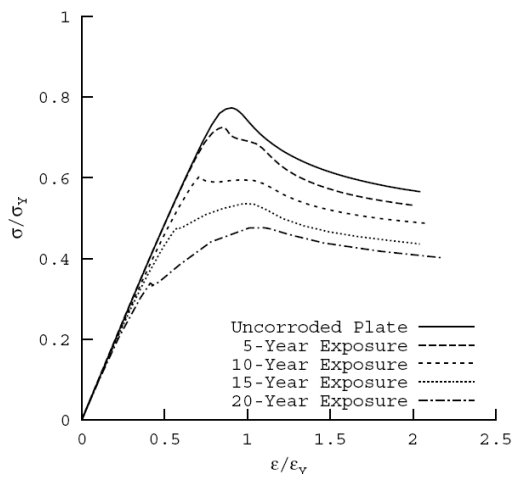


Figure 13 Comparison of average stress-average strain relationships for a plate with random distribution of corrosion ($a = 1600$ mm, $b = 800$ mm, $t = 14$ mm, $S = 0.23$).

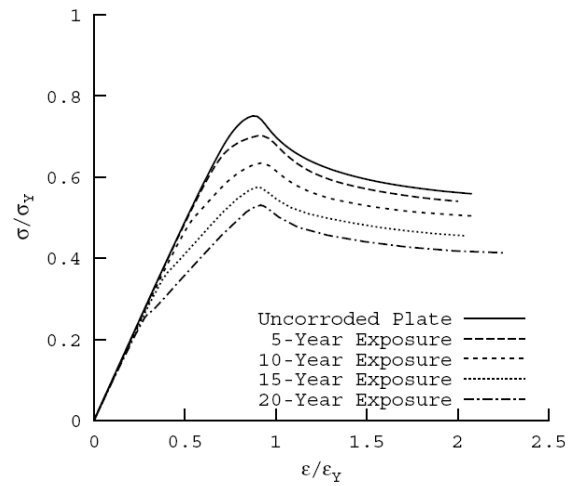


Figure 14 Comparison of average stress-average strain relationships for a plate with random distribution of corrosion ($a = 2400$ mm, $b = 800$ mm, $t = 14$ mm, $S = 0.23$).

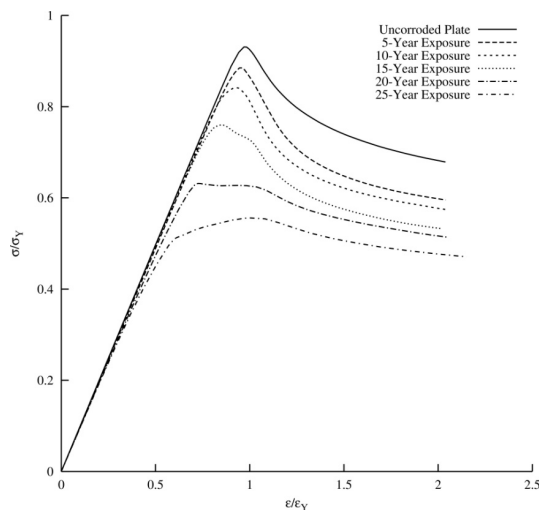


Figure 15 Comparison of average stress-average strain relationships for a plate with random distribution of corrosion ($a = 1600$ mm, $b = 800$ mm, $t = 18$ mm, $S = 0.23$).

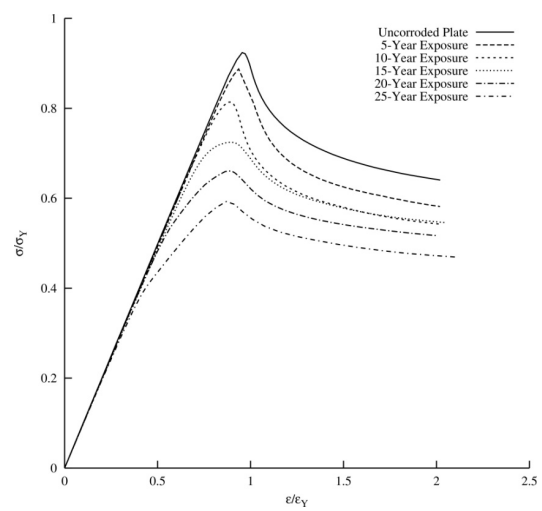


Figure 16 Comparison of average stress-average strain relationships for a plate with random distribution of corrosion ($a = 2400$ mm, $b = 800$ mm, $t = 18$ mm, $S = 0.23$).

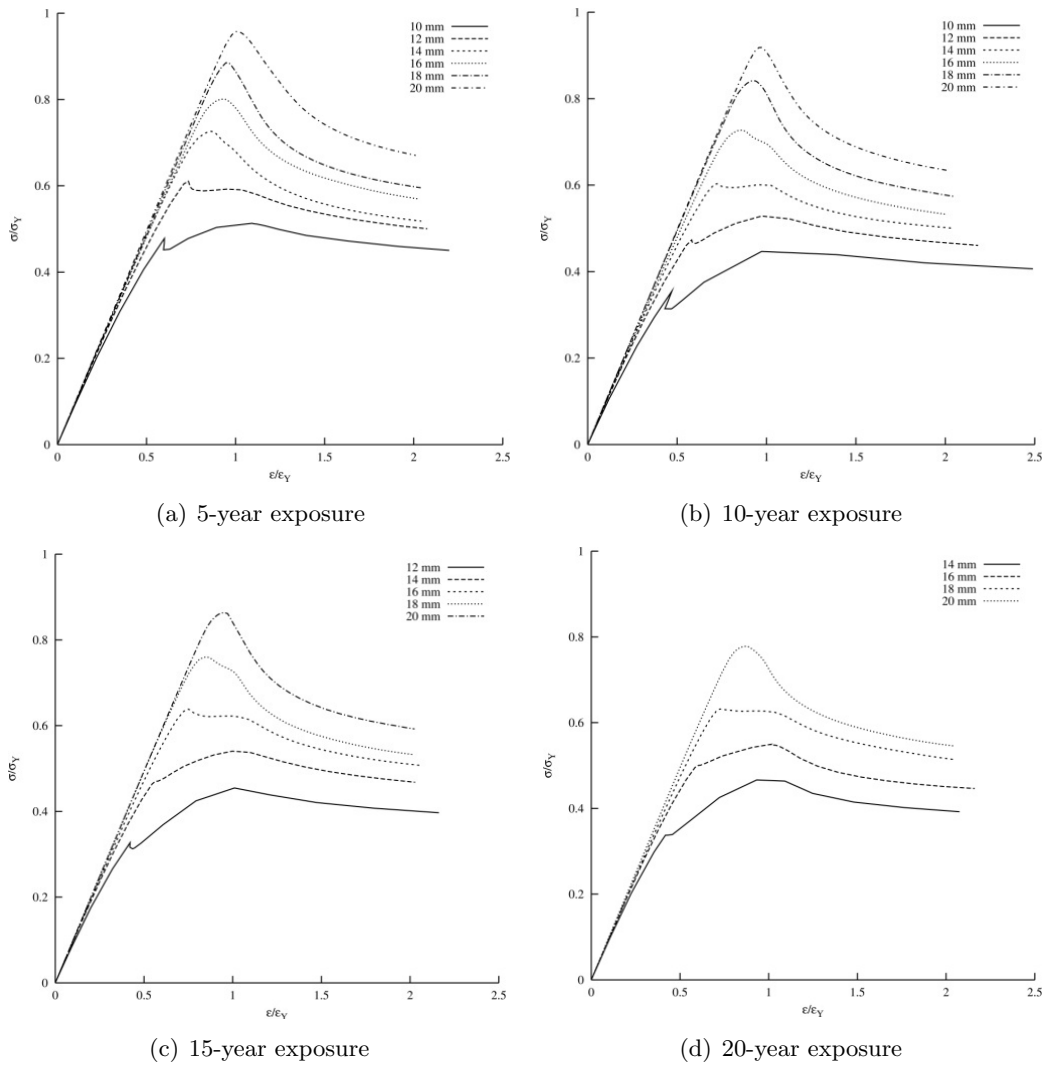


Figure 17 Comparison of average stress-average strain relationships for a plate with random distribution of corrosion ($a = 1600$ mm, $b = 800$ mm, $t = 10$ - 20 mm, $S = 0.23$).

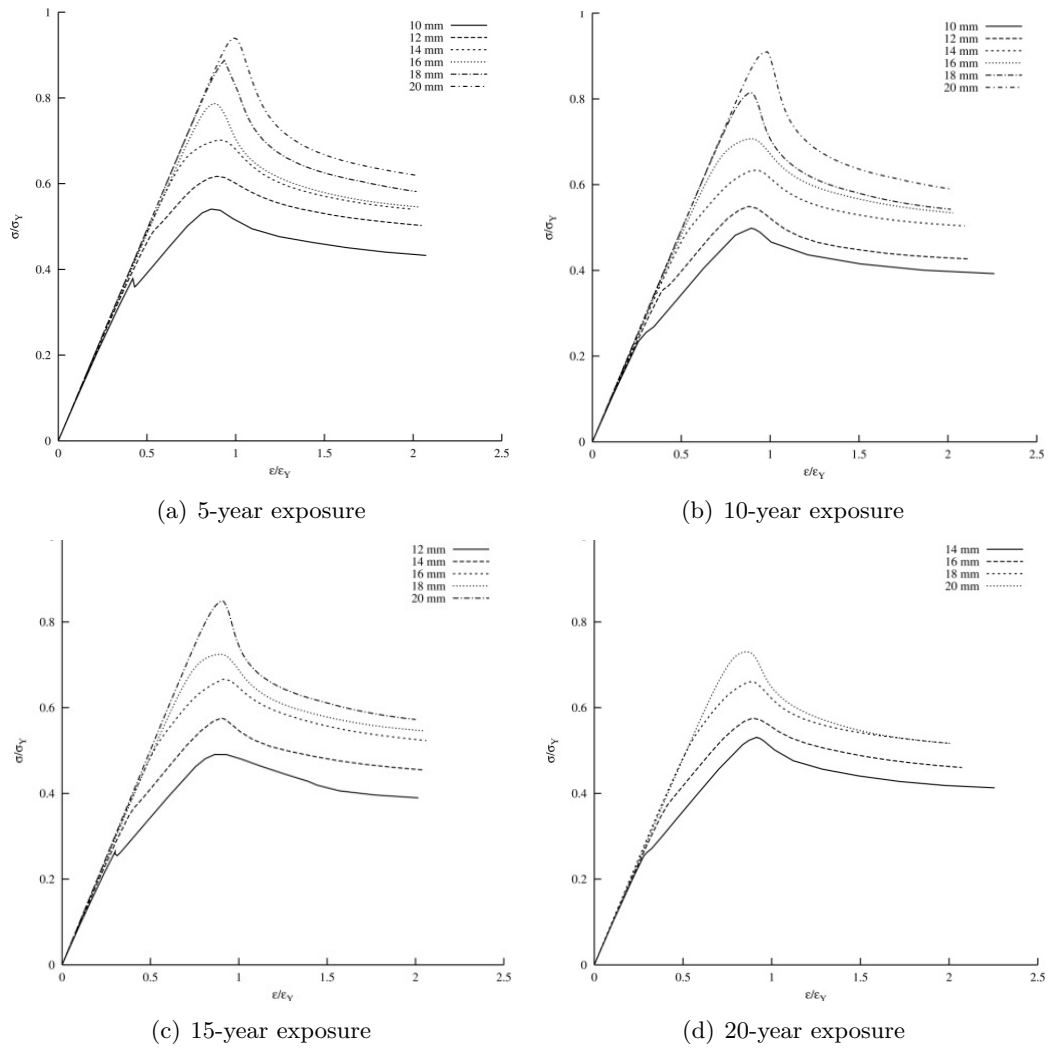


Figure 18 Comparison of average stress-average strain relationships for a plate with random distribution of corrosion ($a = 2400$ mm, $b = 800$ mm, $t = 10$ -20 mm, $S = 0.23$).

5.2 Stiffened plate models

For each of the above-mentioned cases, 50 models were created changing the random thickness variation parameters. The corroded surfaces of the models were different in these cases. Gaussian distribution for random thickness variation was considered in all cases and corresponding models. All of the stiffened plate models were analysed under longitudinal in-plane compression. Average stress-average strain relationships for the stiffened plate models with flat-bar, tee-bar and angle-bar stiffeners are respectively shown in Fig. 19, Fig. 20 and Fig. 21. Also, Von Mises stress distributions and deflection modes at ultimate strength level and final step of calculations are shown for a selection of the cases in Tables 13, 14 and 15.

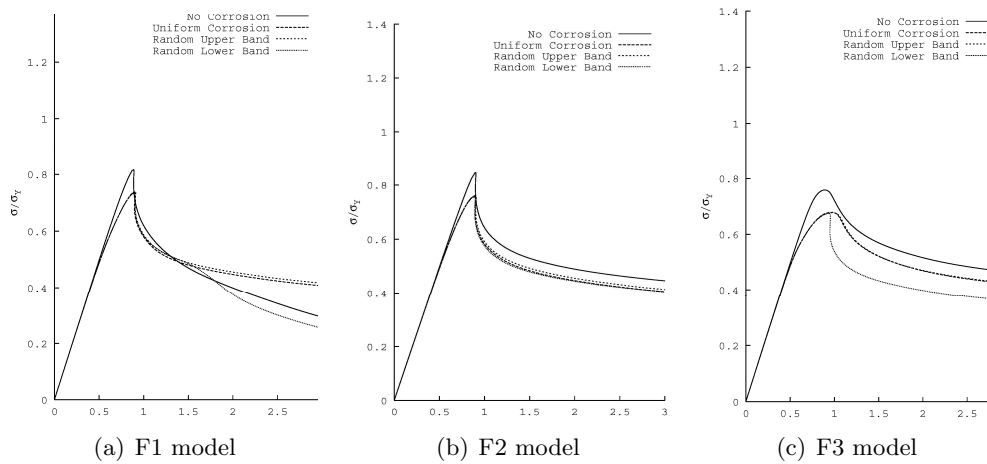


Figure 19 Comparison of average stress-average strain relationships for corroded stiffened plates with $AR = 3$, $t = 13$ mm, stiffener type F , mean corrosion depth = 2mm and $S = 0.2$ mm made of NS steel.

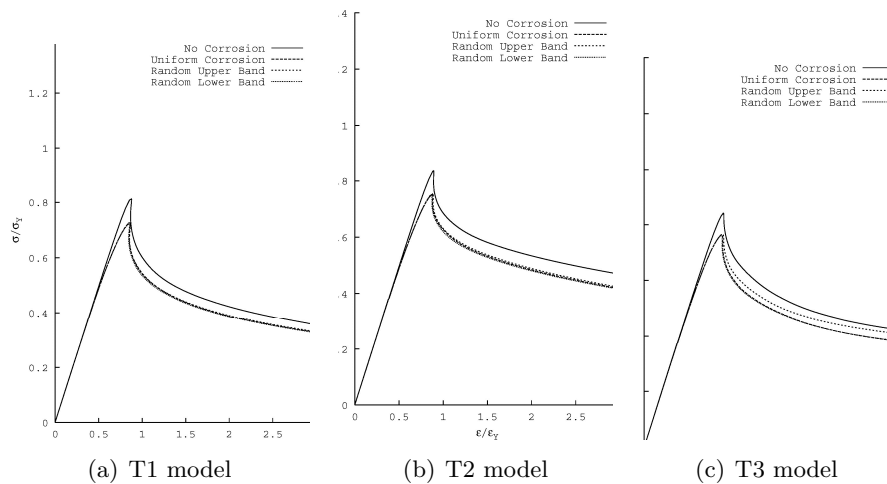


Figure 20 Comparison of average stress-average strain relationships for corroded stiffened plates with $AR = 3$, $t = 13$ mm, stiffener type T , mean corrosion depth = 2mm and $S = 0.2$ mm made of NS steel.

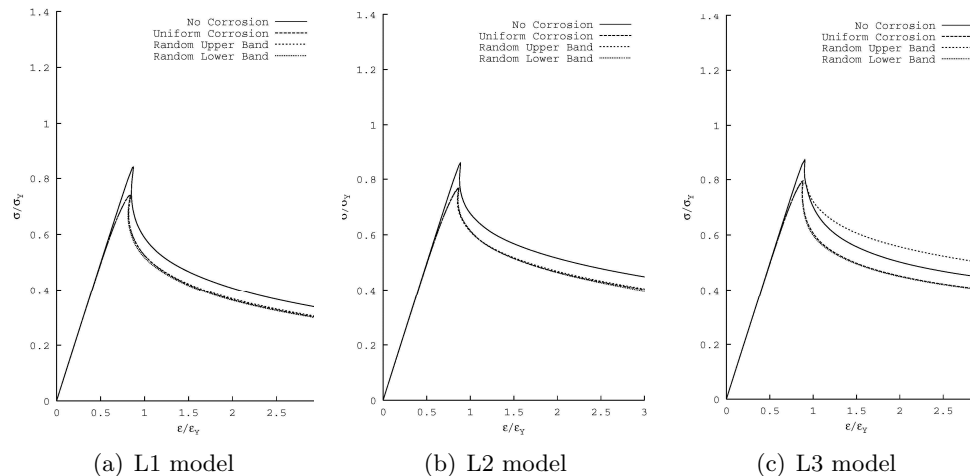


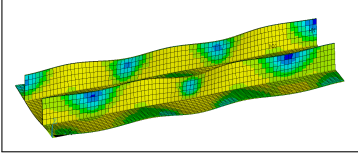
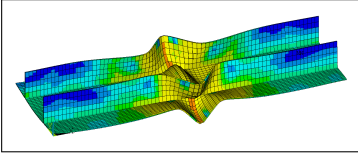
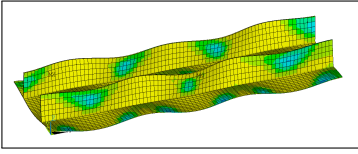
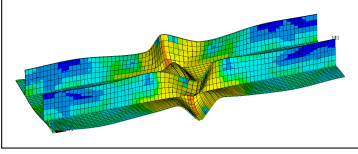
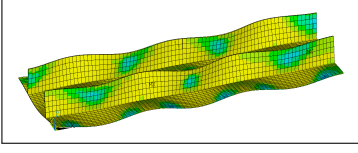
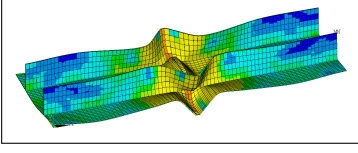
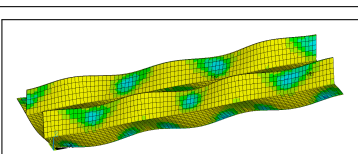
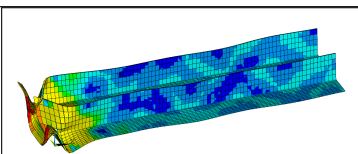
Figure 21 Comparison of average stress-average strain relationships for corroded stiffened plates with $AR = 3$, $t = 13$ mm, stiffener type L , mean corrosion depth = 2mm and $S = 0.2$ mm made of NS steel.

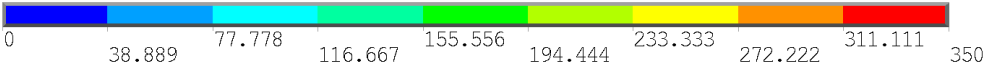
The maximum magnitude of thin-horse mode initial deflection for the plate part in corroded models is calculated using Eq. (5) based on the original thickness of the plate. The average stress-average strain relationships of the stiffened plate models in un-corroded condition as well as in the condition of having uniform thickness reduction are shown in Figs. 19 to 21. The stiffened plate in the condition of uniform corrosion or uniform thickness reduction has a reduction equal to the mean corrosion depth from original un-corroded thickness for its plate and stiffener parts.

Figures 19 to 21 in addition to the results summarised in Tables 13 to 15 reveal the following main characteristics for the buckling/ultimate strengths and behaviours of the corroded stiffened plate models

- Random thickness variations in the stiffened plate model surfaces mainly affect their post-ultimate-strength regimes while their pre-ultimate-strength behaviours are almost unchanged. When the average stress-average strain relationships of 50 models analysed in any case are drawn, their post-ultimate-strength regions create a band. Such a band in post-ultimate-strength regions has a lower limit and an upper limit.
- The curve of average stress-average strain for the condition of uniformly corroded stiffened plate model lies inside the band of average stress-average strain relationships of corresponding randomly corroded models. This can be well understood by paying attention to Figs. 19 to 21 where the curve of uniformly corroded stiffened plate model is seen to be in between the curves, corresponding to upper and lower limits of the bands in each of the analysed cases. In other words, the curve of the uniformly corroded stiffened plate model may be regarded as the practical mean curve representing the average stress-average strain relationship of the randomly corroded stiffened plate models in each case. Of course, there are some exceptions among the results where the curve of uniformly corroded stiffened plate model approaches to the upper or lower limits of the band.

Table 13 A selection of stress distributions and deflection modes for corroded stiffened plate model F3 at ultimate strength level and final step of calculations (magnification factor for deflection mode: 10).

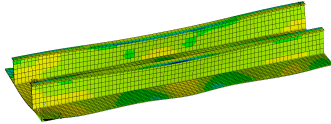
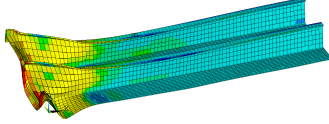
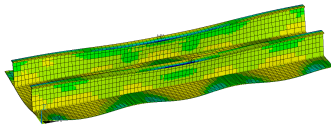
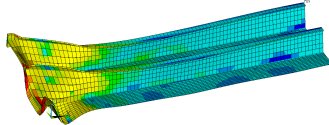
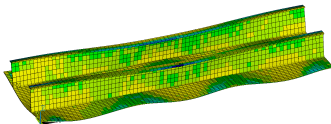
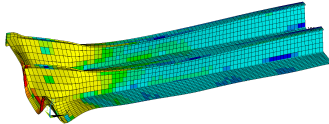
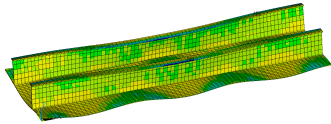
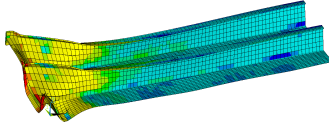
Plate 2400 × 800 × 13, F3 model, 2mm Corrosion, S=0.2 mm, NS steel				
Case	Ultimate strength step	$\frac{\sigma_{ave}}{\sigma_Y}$	Final Step $\frac{\epsilon}{\epsilon_Y} = 3$	$\frac{\sigma_{ave}}{\sigma_Y}$
No Corrosion		0.759		0.462
Uniform Corrosion		0.678		0.421
Random Upper Band		0.678		0.423
Random Lower Band		0.675		0.358




0 38.889 77.778 116.667 155.556 194.444 233.333 272.222 311.111 350

- The trends of the curves in the post-ultimate-strength regions are not always entirely similar to each other. In some cases, local descending or ascending behaviours are observed on the post-ultimate-strength regions of the average stress-average strain curves.
- The mode shapes and Von Mises stress contours shown in Tables 13 to 15 reveal that almost regular half-waves are generated inside the stiffened plate components in longitudinal direction at the ultimate strength level. Besides, post-ultimate-strength mode shapes show that local accumulation of deflection in some regions of the model in addition to the unloading the rest of model are occurred. The place of local deflection accumulation is not fixed and, in other words, changes from case to case.
- In all cases, a remarkable drop in the value of ultimate strength and buckling strength of the stiffened plate models, as a result of random general corrosion is seen. Also, the results show that the ultimate strain does not alter so much as the stiffened plate models

Table 14 A selection of stress distributions and deflection modes for corroded stiffened plate model T3 at ultimate strength level and final step of calculations (magnification factor for deflection mode: 10).

Plate 2400 × 800 × 13, T3 model, 2mm Corrosion, S=0.2 mm, NS steel				
Case	Ultimate strength step	$\frac{\sigma_{ave}}{\sigma_Y}$	Final Step $\frac{\varepsilon}{\varepsilon_Y} = 3$	$\frac{\sigma_{ave}}{\sigma_Y}$
No Corrosion		0.841		0.418
Uniform Corrosion		0.764		0.376
Random Upper Band		0.766		0.404
Random Lower Band		0.762		0.377



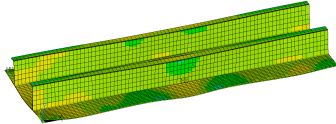
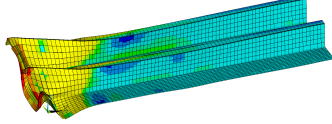
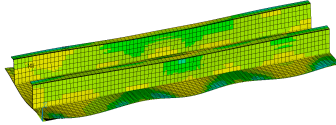
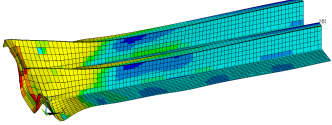
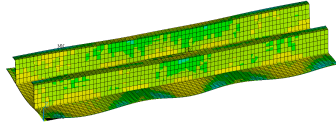
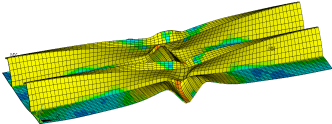
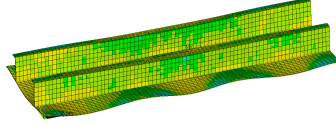
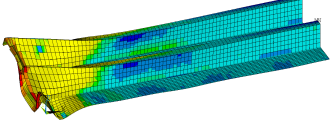
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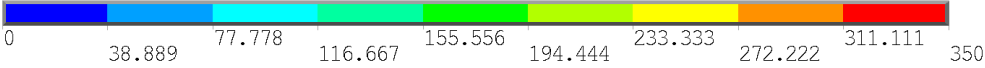
suffer from random general corrosion.

6 CONCLUSIONS

A series of nonlinear elastic-plastic finite element analyses has been performed on the plates and stiffened plates in different conditions of un-corroded and randomly corroded. The models have been subjected to in-plane compression load. Full-range average stress-average strain relationships of the plates have been derived considering changes in plate aspect ratio and plate slenderness or thickness. This is while; the average stress-average strain relationships of the stiffened plates have been derived considering the changes in stiffened plate characteristics, mean corrosion depth and standard deviation of random thickness variation. Some of the

Table 15 A selection of stress distributions and deflection modes for corroded stiffened plate model L3 at ultimate strength level and final step of calculations (magnification factor for deflection mode: 10).

Plate 2400 × 800 × 13, L3 model, 2mm Corrosion, S=0.2 mm, NS steel				
Case	Ultimate strength step	$\frac{\sigma_{ave}}{\sigma_Y}$	Final Step $\frac{\epsilon}{\epsilon_Y} = 3$	$\frac{\sigma_{ave}}{\sigma_Y}$
No Corrosion		0.871		0.444
Uniform Corrosion		0.795		0.401
Random Upper Band		0.791		0.495
Random Lower Band		0.790		0.398



0 38.889 77.778 116.667 155.556 194.444 233.333 272.222 311.111 350

outcomes can be summarised as follows:

- Aspect ratio and thickness (slenderness) of the plate have different effects on the strength characteristics of the corroded plate.
- Age or sea exposure time of the plate models affects mainly their post-buckling-strength regimes and degrades their buckling/ultimate strength.
- Snap-back behaviours are seen in the average stress-average strain relationships of the corroded plate elements, especially when their slenderness parameter falls to the range of thin plates.
- Reduction in the buckling strength of both-sides randomly corroded steel plates is generally higher than the reduction in their ultimate strength. The ratio of buckling strength

to the ultimate strength at a specific exposure time may be sometimes about 2.

- Random thickness variations in the stiffened plate model surfaces mainly affect their post-ultimate-strength regimes while their pre-ultimate-strength behaviours are almost unchanged.
- The condition of uniformly corroded stiffened plate almost in all cases exhibits an intermediate condition for randomly corroded stiffened plates.
- A remarkable drop in the value of ultimate strength and buckling strength of the stiffened plate models, as a result of random general corrosion is seen.

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